

**MODELLING BIOLOGICAL MACROMOLECULES IN SOLUTION:
THE GENERAL TRI-AXIAL ELLIPSOID**

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Appendix V FORTRAN IV computer programs

- Program 1: Evaluates values of the various hydrodynamic shape functions for tri-axial ellipsoids for a user specifiable value of the axial ratios (a/b , b/c)
- Program 2: Produces tables of these functions for axial ratios between 1.0 and 2.0 in steps of 0.1
- Program 3: Produces a contour map of v in the (a/b , b/c) plane for axial ratios between 1.0 and 3.0
- Program 4: Produces plots of the various tri-axial functions in the (a/b , b/c) plane corresponding to the point (1.5, 1.5). Several plots allow for arbitrary errors in measurement
- Program 5: Non-linear least squares iterative method for resolving a 2-term exponential birefringence decay. This program (and the following two) produces its own synthetic data
- Program 6: Fourier Transform solution of the Laplace Integral Equation method
- Program 7: R-constrained non-linear least squares iterative method

<u>Function</u>	<u>Computer Symbol</u>
a/b	A/B
b/c	B/C
v	NU, S
$f/f_o (\equiv P)$	F
ζ_a/ζ_o	CA, CA/CO
ζ_b/ζ_o	CB, CB/CO
ζ_c/ζ_o	CC, CC/CO
ϱ_a/ϱ_o	RHOA, RHOA/RHOO
ϱ_b/ϱ_o	RHOB, RHOB/RHOO
ϱ_c/ϱ_o	RHOC, RHOC/RHOO
β	BETA
R	R
δ_a	DELTA A, DELTA(A)
δ_b	DELTA B, DELTA(B)
δ_c	DELTA C, DELTA(C)
γ_a	GAMMA A, GAMMA(A)
γ_b	GAMMA B, GAMMA(B)
γ_c	GAMMA C, GAMMA(C)
μ_a	MUA, MU(A)
μ_b	MUB, MU(B)
μ_c	MUC, MU(C)
τ_h/τ_o	TAU, TAU/TAUO
ψ	PSI
Λ	LAMBDA
θ_+^{red}	TPLS, THETA+, Z
θ_-^{red}	TMNS, THETA-, U

<u>Function</u>	<u>Computer Symbol</u>
δ_+	DPLS, DELTA+, V
δ_-	DMNS, DELTA-, W
γ_+	GPLS, GAMMA+
γ_-	GMNS, GAMMA-
τ_1/τ_0	T1
τ_2/τ_0	T2
τ_3/τ_0	T3
τ_4/τ_0	T4
τ_5/τ_0	T5
θ_+	THPLUS
θ_-	THMNUS

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C      *** *****
C      THIS PROGRAM GENERATES VALUES OF THE VARIOUS HYDRODYNAMIC
C      SHAPE FUNCTIONS FOR A USER SPECIFIABLE VALUE OF THE AXIAL
C      RATIOS A/B (=N1) & B/C (=N2)
C      *****
C      PROGRAM MAIN(INPUT,OUTPUT,TAPE2=INPUT,TAPE3=OUTPUT)
C      COMMON/PARAM/A,C,NN
C      EXTERNAL FUN
C      DIMENSION ALPHA(10)
C      REAL NU,M,O,P
C      REAL MUA,MUB,MUC,PSI,N1,N2,RHOA,RHOB,RHOC
C ENTER AS DATA AT THE FOOT OF THE PROGRAM (A/B, B/C)
      READ(2,*)N1,N2
      NN=0
C      COMPUTE THE ELLIPTIC INTEGRALS
      DO45 K=1,10
      A=N1
      B=1.0
      C=1.0/N2
      NN=NN+1
C      SET LIMITS FOR NUMERICAL INTEGRATION (THESE LIMITS
C      BELOW HAVE BEEN PREVIOUSLY TESTED FOR CONVERGENCE)
      AA=0.0
      BB=1000000
      IF(NN.EQ.10)BB=500000000
      MAXDIV=50
      EPS=1.0E-08
      ACC=0.0
      IFAIL=0
C      CALL U.K. "NAG" LIBRARY ROUTINE FOR NUMERICAL EVALUATION
C      OF THE INTEGRALS "ALPHA" GIVEN IN THE SUBROUTINE BELOW
      CALL D01AGF(AA,BB,FUN,MAXDIV,EPS,ACC,ANS,ERROR,NOFUN,IFAIL)
      ALPHA(NN)=ANS
45 CONTINUE
      B=1.0
C      NOW COMPUTE THE FUNCTION VALUES USING THE STORED INTEGRAL VALUES
      NU=(1.0/(A*B*C))*((4.0/15.0)*((ALPHA(7)+ALPHA(8)
+ +ALPHA(9))/((ALPHA(8)*ALPHA(9)+ALPHA(9)*ALPHA
+ (7)+ALPHA(7)*ALPHA(8)))+(1.0/5.0)*(((ALPHA(2)
+ +ALPHA(3))/((ALPHA(4)*(B*B*ALPHA(2)+C*C*ALPHA(3)
+ )))+(ALPHA(3)+ALPHA(1))/(ALPHA(5)*(C*C*ALPHA(3)
+ +A*A*ALPHA(1))))+(ALPHA(1)+ALPHA(2))/(ALPHA(6)
+ *(A*A*ALPHA(1)+B*B*ALPHA(2))))))
      M=(B*B+C*C)/((B*B*ALPHA(2)+C*C*ALPHA(3))
      O=(C*C+A*A)/((C*C*ALPHA(3)+A*A*ALPHA(1))
      P=(A*A+B*B)/((A*A*ALPHA(1)+B*B*ALPHA(2))
      TPLS=((A*B*C)/(12.0))*(((1.0/M)+(1.0/O)+(1.0/P
+ ))+(((1.0/M**2.0)+(1.0/O**2.0)+(1.0/P**2.0))-
+ ((1.0/(M*O)))+(1.0/(O*P)))+(1.0/(P*M
+ ))))*0.5))
      TMNS=((A*B*C)/(12.0))*(((1.0/M)+(1.0/O)+(1.0/P
+ ))-(((1.0/M**2.0)+(1.0/O**2.0)+(1.0/P**2.0))-
+ ((1.0/(M*O)))+(1.0/(O*P)))+(1.0/(P*M
+ ))))*0.5))
      DPLS=6.0*TPLS*NU
      DMNS=6.0*TMNS*NU
      F=2.0/(((A*B*C)**(1.0/3.0))*ALPHA(10))
      R=2.0*(1.0+(F**3.0))/NU
      BETA=((1.0/1000000.0)*(((6.0249**((1.0/3.0))*(10.0**((23.0/3.0
+ )))/(16200.0*3.141592654*3.141592654)**(1.0/3.0)))*(NU
+ **((1.0/3.0))/F
      CA=(2.0/(3.0*A*B*C))*M
      CB=(2.0/(3.0*A*B*C))*O
      CC=(2.0/(3.0*A*B*C))*P
      RHOA=2.0/((1.0/CB)+(1.0/CC))
      RHOB=2.0/((1.0/CC)+(1.0/CA))
      RHOC=2.0/((1.0/CA)+(1.0/CB))
      DELA=NU/CA
      DELB=NU/CB
      DELC=NU/CC
      TAU=3.0/((1.0/CA)+(1.0/CB)+(1.0/CC))
      PSI=F*((1.0/TAU)**(1.0/3.0))
      V=NU/TAU
      ZZ=(1.0/2.0)*(F**3.0)
      GAMMAA=ZZ*((1.0/CB)+(1.0/CC))
      GAMMAB=ZZ*((1.0/CC)+(1.0/CA))
      GAMMAC=ZZ*((1.0/CA)+(1.0/CB))
      MUA=(CA**((1.0/3.0)))/F
      MUB=(CB**((1.0/3.0)))/F
      MUC=(CC**((1.0/3.0)))/F
      GPLS=6.0*TPLS*(F**3.0)

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GMNS=6.0*TMNS*(F**3.0)
X1=0.5*((1.0/RHOB)+(1.0/RHOC)-(1.0/RHOA))
X2=0.5*((1.0/RHOC)+(1.0/RHOA)-(1.0/RHOB))
X3=0.5*((1.0/RHOA)+(1.0/RHOB)-(1.0/RHOC))
X4=(X1+X2+X3)/3.0
X5=((X1**2.0)+(X2**2.0)+(X3**2.0)-(X1*X2)-(X2*X3)-(X3*X1))
+**0.5
T1=1.0/(X4+X1)
T2=1.0/(X4+X2)
T3=1.0/(X4+X3)
T4=3.0/((6.0*X4)-(2.0*X5))
T5=3.0/((6.0*X4)+(2.0*X5))
WRITE(3,97)
97 FORMAT( " ")
WRITE(3,98)
98 FORMAT( " ")
WRITE(3,99) A,1/C
99 FORMAT( 5X," A/B "F7.2," B/C ",F7.2)
WRITE(3,100) NU
100 FORMAT( 5X," NU ",F10.5)
WRITE(3,106) F
106 FORMAT( 5X," F ",F10.5)
WRITE(3,101) TPLS
101 FORMAT( 5X," THETA+ ",F15.5)
WRITE(3,102) TMNS
102 FORMAT( 5X," THETA- ",F15.5)
WRITE(3,103) DPLS
103 FORMAT( 5X," DELTA+ ",F15.5)
WRITE(3,104) DMNS
104 FORMAT( 5X," DELTA- ",F15.5)
WRITE(3,105) R
105 FORMAT( 5X," R ",F15.5)
WRITE(3,107) BETA
107 FORMAT( 5X," BETA ",F15.5)
WRITE(3,202)
202 FORMAT( 5X,"THE 3 ROTATIONAL FRICTIONAL RATIOS:")
WRITE(3,108) CA
108 FORMAT( 5X," CA ",F15.5)
WRITE(3,109) CB
109 FORMAT( 5X," CB ",F15.5)
WRITE(3,110) CC
110 FORMAT( 5X," CC ",F15.5)
WRITE(3,203)
203 FORMAT( 5X,"THE 3 ROTATIONAL RELAXATION TIME RATIOS:")
WRITE(3,111) RHOA
111 FORMAT( 5X," RHOA ",F15.5)
WRITE(3,112) RHOB
112 FORMAT( 5X," RHOB ",F15.5)
WRITE(3,113) RHOC
113 FORMAT( 5X," RHOC ",F15.5)
WRITE(3,114) DELA
114 FORMAT( 5X," DELTAA ",F15.5)
WRITE(3,115) DELB
115 FORMAT( 5X," DELTAB ",F15.5)
WRITE(3,116) DELC
116 FORMAT( 5X," DELTAC ",F15.5)
WRITE(3,204)
204 FORMAT( 5X,"THE HARMONIC MEAN RELAXATION TIME RATIO:")
WRITE(3,117) TAU
117 FORMAT( 5X," TAU ",F15.5)
WRITE(3,118) PSI
118 FORMAT( 5X," PSI ",F15.5)
WRITE(3,119) V
119 FORMAT( 5X," LAMBDA ",F15.5)
WRITE(3,120) GAMMAA
120 FORMAT( 5X," GAMMAA ",F15.5)
WRITE(3,121) GAMMAB
121 FORMAT( 5X," GAMMAB ",F15.5)
WRITE(3,122) GAMMAC
122 FORMAT( 5X," GAMMAC ",F15.5)
WRITE(3,123) MUA
123 FORMAT( 5X," MUA ",F15.5)
WRITE(3,124) MUB
124 FORMAT( 5X," MUB ",F15.5)
WRITE(3,125) MUC
125 FORMAT( 5X," MUC ",F15.5)
WRITE(3,126) GPLS
126 FORMAT( 5X," GAMMA+ ",F15.5)
WRITE(3,127) GMNS
127 FORMAT( 5X," GAMMA- ",F15.5)
WRITE(3,201)

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201 FORMAT( 5X,"FLUORESCENCE ANISOTROPY RELAXATION TIME RATIOS:")
WRITE(3,130)T1
130 FORMAT( 5X,"      T1      ",F15.5)
WRITE(3,131)T2
131 FORMAT( 5X,"      T2      ",F15.5)
WRITE(3,132)T3
132 FORMAT( 5X,"      T3      ",F15.5)
WRITE(3,133)T4
133 FORMAT( 5X,"      T4      ",F15.5)
WRITE(3,134)T5
134 FORMAT( 5X,"      T5      ",F15.5)
STOP
END

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CCC

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REAL FUNCTION FUN(X)
COMMON/PARAM/A,C,NN
B=1.0
GOTO(10,20,30,40,50,60,70,80,90,100),NN
10 FUN=1/((A*A+X)**1.5*(B*B+X)**0.5*(C*C+X)**0.5)
RETURN
20 FUN=1/((A*A+X)**0.5*(B*B+X)**1.5*(C*C+X)**0.5)
RETURN
30 FUN=1/((A*A+X)**0.5*(B*B+X)**0.5*(C*C+X)**1.5)
RETURN
40 FUN=1/((A*A+X)**0.5*(B*B+X)**1.5*(C*C+X)**1.5)
RETURN
50 FUN=1/((A*A+X)**1.5*(B*B+X)**0.5*(C*C+X)**1.5)
RETURN
60 FUN=1/((A*A+X)**1.5*(B*B+X)**1.5*(C*C+X)**0.5)
RETURN
70 FUN=X/((A*A+X)**0.5*(B*B+X)**1.5*(C*C+X)**1.5)
RETURN
80 FUN=X/((A*A+X)**1.5*(B*B+X)**0.5*(C*C+X)**1.5)
RETURN
90 FUN=X/((A*A+X)**1.5*(B*B+X)**1.5*(C*C+X)**0.5)
RETURN
100 FUN=1.0/(((A*A+X)*(B*B+X)*(C*C+X))**0.5)
RETURN
END

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Program 1 Results

A/B	1.50	B/C	1.50
NU	2.89170		
F	1.04410		
THETA+		.16261	
THETA-		.11622	
DELTA+		2.82127	
DELTA-		2.01645	
R	1.47887		
BETA	2.12334		
THE 3 ROTATIONAL FRICTIONAL RATIOS:			
CA	.89762		
CB	1.39800		
CC	1.47041		
THE 3 ROTATIONAL RELAXATION TIME RATIOS:			
RHOA	1.43329		
RHOB	1.11474		
RHOC	1.09327		
DELTAA	3.22152		
DELTAB	2.06846		
DELTAC	1.96660		
THE HARMONIC MEAN RELAXATION TIME RATIO:			
TAU	1.19548		
PSI	.98378		
LAMBDA	2.41886		
GAMMAA	.79414		
GAMMAB	1.02107		
GAMMAC	1.04112		
MUA	.92389		
MUB	1.07092		
MUC	1.08910		
GAMMA+	1.11051		
GAMMA-	.79372		
FLUORESCENCE ANISOTROPY RELAXATION TIME RATIOS:			
T1	1.02536		
T2	1.28883		
T3	1.31877		
T4	1.43405		
T5	1.02497		

Program 2

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*****
THIS PROGRAM COMPUTES TABLES OF THE VISCOSITY INCREMENT NU,
THE TRANSLATIONAL FRICTIONAL RATIO (F/F0), THE ROTATIONAL
FRICTIONAL RATIOS( CA/CO, CB/CO, CC/CO ), THE ROTATIONAL
RELAXATION TIME RATIOS(RHOA/RHO0, RHOB/RHO0, RHOC/RHO0), THE
HARMONIC MEAN RELAXATION TIME RATIO( TAU/TAU0 ), THE RIDGEWAY
ELECTRIC BIREFRINGENCE DECAY CONSTANTS( THETA+, THETA-), AND
THEIR CORRESPONDING SWELLING - INDEPENDENT FUNCTIONS:
R, BETA, DELTAA, DELTAB, DELTAC, GAMMAA, GAMMAB, GAMMAC,
MUA, MUB, MUC, PSI, DELTA+, DELTA-, GAMMA+ AND GAMMA-
AS FUNCTIONS OF THE AXIAL RATIOS A/B, B/C, IN THE RANGE 1.0 TO
2.0 IN STEPS OF 0.1, FOR A GENERAL TRIAXIAL ELLIPSOID PARTICLE
MODEL. ( THE SUBSCRIPT "0" REFERS TO THE CORRESPONDING COEFFICIENT
FOR A SPHERE OF EQUAL VOLUME )
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PROGRAM MAIN(INPUT,OUTPUT,TAPE2=INPUT,TAPE3=OUTPUT)
COMMON/PARAM/A,C,NN
EXTERNAL FUN
DIMENSION ALPHA(10,11,11),NU(11,11),F(11,11),R(11,11),H(11,11)
+ ,BETA(11,11),CA(11,11),CB(11,11),CC(11,11),M(11,11),O(11,11)
+ ,P(11,11),TPLS(11,11),TMNS(11,11),RHOA(11,11),RHOB(11,11)
+ ,RHOC(11,11),TAU(11,11),PSI(11,11),DELA(11,11),DELB(11,11)
+ ,DELC(11,11),GAMMAA(11,11),GAMMAB(11,11),GAMMAC(11,11),MUA(11,11)
+ ,MUB(11,11),MUC(11,11),DPLS(11,11),DMNS(11,11),GPLS(11,11)
+ ,GMNS(11,11),Y(11),Z(11),ZZ(11,11)
REAL NU,M,O,P,MUA,MUB,MUC,PSI
COMPUTE THE ELLIPTIC INTEGRALS
NN=0
DO45 K=1,10
A=0.9
NN=NN+1
DO40 I=1,11
A=A+0.1
C=1.0/0.9
DO30 N=1,11
C=C/(1.0+0.1*C)
SET LIMITS FOR NUMERICAL INTEGRATION (THESE LIMITS
BELOW HAVE BEEN PREVIOUSLY TESTED FOR CONVERGENCE)
AA=0.0
BB=1000000
IF(NN.EQ.10) BB=500000000
MAXDIV=50
EPS=1.0E-08
ACC=0.0
IFAIL=0
CALL U.K. "NAG" LIBRARY ROUTINE FOR NUMERICAL EVALUATION
OF THE INTEGRALS "ALPHA" GIVEN IN THE SUBROUTINE BELOW
CALL D01AGF(AA,BB,FUN,MAXDIV,EPS,ACC,ANS,ERROR,NOFUN,IFAIL)
ALPHA(NN,I,N)=ANS
30 CONTINUE
40 CONTINUE
45 CONTINUE
B=1.0
A=0.9
DO80 J=1,11
A=A+0.1
Y(J)=A
C=1.0/0.9
DO70 N=1,11
C=C/(1.0+0.1*C)
Z(N)=1/C
NOW COMPUTE THE FUNCTION VALUES USING THE STORED INTEGRAL VALUES
NU(J,N)=(1.0/(A*B*C))*((4.0/15.0)*((ALPHA(7,J,N)+ALPHA(8,J,N)
+ ALPHA(9,J,N))/(ALPHA(8,J,N)*ALPHA(9,J,N)+ALPHA(9,J,N)*ALPHA
+ (7,J,N)+ALPHA(7,J,N)*ALPHA(8,J,N)))+(1.0/5.0)*((ALPHA(2,J,N)
+ ALPHA(3,J,N))/(ALPHA(4,J,N)*(B*B*ALPHA(2,J,N)+C*C*ALPHA(3,J,N)
+ )))+(ALPHA(3,J,N)+ALPHA(1,J,N))/(ALPHA(5,J,N)*(C*C*ALPHA(3,J,N)
+ A*A*ALPHA(1,J,N)))+(ALPHA(1,J,N)+ALPHA(2,J,N))/(ALPHA(6,J,N)
+ A*A*ALPHA(1,J,N)+B*B*ALPHA(2,J,N))))
F(J,N)=2.0/((A*B*C)**(1.0/3.0))*ALPHA(10,J,N)
R(J,N)=2.0*(1.0+(F(J,N)**3.0))/NU(J,N)
BETA(J,N)=(1.0/1000000.0)*((6.0249**((1.0/3.0)*(10.0**((23.0/3.0
+ )))/(16200.0*3.141592654*3.141592654)**(1.0/3.0)))*(NU(J,N)
+ *(1.0/3.0))/F(J,N)
M(J,N)=(B*B+C*C)/(B*B*ALPHA(2,J,N)+C*C*ALPHA(3,J,N))
O(J,N)=(C*C+A*A)/(C*C*ALPHA(3,J,N)+A*A*ALPHA(1,J,N))
P(J,N)=(A*A+B*B)/(A*A*ALPHA(1,J,N)+B*B*ALPHA(2,J,N))
TPLS(J,N)=(A*B*C)/(12.0)*(((1.0/M(J,N)))+(1.0/O(J,N)))+(1.0/P(J,
+ N)))+(((1.0/M(J,N)**2.0)+(1.0/O(J,N)**2.0)+(1.0/P(J,N)**2.0))-

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+ ((1.0/(M(J,N)*O(J,N)))+(1.0/(O(J,N)*P(J,N)))+(1.0/(P(J,N)*M(J,
+ N)))))*0.5))
+ N)))-(((1.0/M(J,N)**2.0)+(1.0/O(J,N)**2.0)+(1.0/P(J,N)**2.0))-
+ ((1.0/(M(J,N)*O(J,N)))+(1.0/(O(J,N)*P(J,N)))+(1.0/(P(J,N)*M(J,
+ N)))))*0.5))
CA(J,N)=(2.0/(3.0*A*B*C))*M(J,N)
CB(J,N)=(2.0/(3.0*A*B*C))*O(J,N)
CC(J,N)=(2.0/(3.0*A*B*C))*P(J,N)
RHOA(J,N)=2.0/((1.0/CB(J,N))+(1.0/CC(J,N)))
RHOB(J,N)=2.0/((1.0/CA(J,N))+(1.0/CC(J,N)))
RHOC(J,N)=2.0/((1.0/CA(J,N))+(1.0/CB(J,N)))
DELA(J,N)=NU(J,N)/CA(J,N)
DELB(J,N)=NU(J,N)/CB(J,N)
DELC(J,N)=NU(J,N)/CC(J,N)
TAU(J,N)=3.0/((1.0/CA(J,N))+(1.0/CB(J,N))+(1.0/CC(J,N)))
PSI(J,N)=F(J,N)*((1.0/TAU(J,N))**3.0)
ZZ(J,N)=(1.0/2.0)*(F(J,N)**3.0)
GAMMAA(J,N)=ZZ(J,N)*((1.0/CB(J,N))+(1.0/CC(J,N)))
GAMMAB(J,N)=ZZ(J,N)*((1.0/CA(J,N))+(1.0/CC(J,N)))
GAMMAC(J,N)=ZZ(J,N)*((1.0/CA(J,N))+(1.0/CB(J,N)))
MUA(J,N)=(CA(J,N)**(1.0/3.0))/F(J,N)
MUB(J,N)=(CB(J,N)**(1.0/3.0))/F(J,N)
MUC(J,N)=(CC(J,N)**(1.0/3.0))/F(J,N)
DPLS(J,N)=6.0*TPLS(J,N)*NU(J,N)
DMNS(J,N)=6.0*TMNS(J,N)*NU(J,N)
GPLS(J,N)=6.0*TPLS(J,N)*(F(J,N)**3.0)
GMNS(J,N)=6.0*TMNS(J,N)*(F(J,N)**3.0)
70 CONTINUE
80 CONTINUE
C THE PROGRAM NOW WRITES OUT THE COMPUTED VALUES IN TABLE FORM
WRITE(3,600)
600 FORMAT(" ")
60 PRINT(3,60)
60 FORMAT("1 A/B B/C NU F/F0 R BETA")
D071 J=1,11
D072 N=1,11
WRITE(3,73)Y(J),Z(N),NU(J,N),F(J,N),R(J,N),BETA(J,N)
73 FORMAT(2F7.1,4F8.3)
72 CONTINUE
71 CONTINUE
WRITE(3,610)
610 FORMAT(" ")
61 PRINT(3,61)
61 FORMAT("1 A/B B/C CA/C0 CB/C0 CC/C0")
D074 J=1,11
D075 N=1,11
WRITE(3,76)Y(J),Z(N),CA(J,N),CB(J,N),CC(J,N)
76 FORMAT(2F7.1,3F8.3)
75 CONTINUE
74 CONTINUE
WRITE(3,620)
620 FORMAT(" ")
62 PRINT(3,62)
62 FORMAT("1 A/B B/C RHOA/RH00 RHOB/RH00 RHOC/RH00")
D081 J=1,11
D082 N=1,11
WRITE(3,83)Y(J),Z(N),RHOA(J,N),RHOB(J,N),RHOC(J,N)
83 FORMAT(2F7.1,3F9.3)
82 CONTINUE
81 CONTINUE
WRITE(3,630)
630 FORMAT(" ")
63 PRINT(3,63)
63 FORMAT("1 A/B B/C DELTA(A) DELTA(B) DELTA(C)")
D084 J=1,11
D085 N=1,11
WRITE(3,86)Y(J),Z(N),DELA(J,N),DELB(J,N),DELC(J,N)
86 FORMAT(2F7.1,3F8.3)
85 CONTINUE
84 CONTINUE
WRITE(3,640)
640 FORMAT(" ")
64 PRINT(3,64)
64 FORMAT("1 A/B B/C GAMMA(A) GAMMA(B) GAMMA(C)")
D091 J=1,11
D092 N=1,11
WRITE(3,93)Y(J),Z(N),GAMMAA(J,N),GAMMAB(J,N),GAMMAC(J,N)
93 FORMAT(2F7.1,3F8.3)
92 CONTINUE
91 CONTINUE

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WRITE(3,650)
650 FORMAT(" ")
PRINT(3,65)
65 FORMAT("1 A/B B/C MU(A) MU(B) MU(C)")
DO94 J=1,11
DO95 N=1,11
WRITE(3,96)Y(J),Z(N),MUA(J,N),MUB(J,N),MUC(J,N)
96 FORMAT(2F7.1,3F8.3)
95 CONTINUE
94 CONTINUE
WRITE(3,660)
660 FORMAT(" ")
PRINT(3,66)
66 FORMAT("1 A/B B/C THETA+ THETA- TAU/TAU0 PSI")
DO101 J=1,11
DO102 N=1,11
WRITE(3,103)Y(J),Z(N),TPLS(J,N),TMNS(J,N),TAU(J,N),PSI(J,N)
103 FORMAT(2F7.1,4F8.3)
102 CONTINUE
101 CONTINUE
WRITE(3,670)
670 FORMAT(" ")
PRINT(3,67)
67 FORMAT("1 A/B B/C DELTA+ DELTA-")
DO104 J=1,11
DO105 N=1,11
WRITE(3,106)Y(J),Z(N),DPLS(J,N),DMNS(J,N)
106 FORMAT(2F7.1,2F8.3)
105 CONTINUE
104 CONTINUE
WRITE(3,680)
680 FORMAT(" ")
PRINT(3,68)
68 FORMAT("1 A/B B/C GAMMA+ GAMMA-")
DO111 J=1,11
DO112 N=1,11
WRITE(3,113)Y(J),Z(N),GPLS(J,N),GMNS(J,N)
113 FORMAT(2F7.1,2F8.3)
112 CONTINUE
111 CONTINUE
WRITE(3,690)
690 FORMAT(" ")
DO114 J=1,11
DO115 N=1,11
115 CONTINUE
114 CONTINUE
STOP
END

```

C
C
C

```

REAL FUNCTION FUN(X)
COMMON/PARAM/A,C,NN
B=1.0
GOTO(10,20,30,40,50,60,70,80,90,100),NN
10 FUN=1/((A*A+X)**1.5*(B*B+X)**0.5*(C*C+X)**0.5)
RETURN
20 FUN=1/((A*A+X)**0.5*(B*B+X)**1.5*(C*C+X)**0.5)
RETURN
30 FUN=1/((A*A+X)**0.5*(B*B+X)**0.5*(C*C+X)**1.5)
RETURN
40 FUN=1/((A*A+X)**0.5*(B*B+X)**1.5*(C*C+X)**1.5)
RETURN
50 FUN=1/((A*A+X)**1.5*(B*B+X)**0.5*(C*C+X)**1.5)
RETURN
60 FUN=1/((A*A+X)**1.5*(B*B+X)**1.5*(C*C+X)**0.5)
RETURN
70 FUN=X/((A*A+X)**0.5*(B*B+X)**1.5*(C*C+X)**1.5)
RETURN
80 FUN=X/((A*A+X)**1.5*(B*B+X)**0.5*(C*C+X)**1.5)
RETURN
90 FUN=X/((A*A+X)**1.5*(B*B+X)**1.5*(C*C+X)**0.5)
RETURN
100 FUN=1.0/((A*A+X)*(B*B+X)*(C*C+X)**0.5)
RETURN
END

```

A/B	B/C	NU	F/FQ	R	BETA
1.0	1.0	2.500	1.000	1.600	2.112
1.0	1.1	2.507	1.001	1.598	2.112
1.0	1.2	2.524	1.003	1.592	2.113
1.0	1.3	2.550	1.006	1.583	2.113
1.0	1.4	2.583	1.010	1.572	2.114
1.0	1.5	2.620	1.014	1.560	2.115
1.0	1.6	2.661	1.019	1.548	2.115
1.0	1.7	2.706	1.025	1.534	2.116
1.0	1.8	2.753	1.030	1.521	2.117
1.0	1.9	2.803	1.036	1.507	2.118
1.0	2.0	2.854	1.042	1.493	2.118
1.1	1.0	2.507	1.001	1.598	2.112
1.1	1.1	2.520	1.002	1.593	2.112
1.1	1.2	2.544	1.005	1.585	2.113
1.1	1.3	2.576	1.009	1.574	2.114
1.1	1.4	2.614	1.014	1.562	2.115
1.1	1.5	2.656	1.019	1.549	2.115
1.1	1.6	2.702	1.024	1.535	2.116
1.1	1.7	2.751	1.030	1.521	2.117
1.1	1.8	2.803	1.036	1.507	2.118
1.1	1.9	2.857	1.042	1.492	2.119
1.1	2.0	2.913	1.049	1.478	2.120
1.2	1.0	2.525	1.003	1.591	2.113
1.2	1.1	2.545	1.005	1.584	2.113
1.2	1.2	2.575	1.009	1.574	2.114
1.2	1.3	2.612	1.013	1.562	2.115
1.2	1.4	2.655	1.018	1.549	2.116
1.2	1.5	2.703	1.024	1.535	2.117
1.2	1.6	2.754	1.030	1.520	2.118
1.2	1.7	2.808	1.036	1.505	2.119
1.2	1.8	2.865	1.043	1.490	2.120
1.2	1.9	2.923	1.049	1.475	2.120
1.2	2.0	2.983	1.056	1.460	2.121
1.3	1.0	2.553	1.006	1.582	2.114
1.3	1.1	2.579	1.009	1.573	2.114
1.3	1.2	2.615	1.013	1.561	2.115
1.3	1.3	2.658	1.018	1.547	2.116
1.3	1.4	2.706	1.024	1.533	2.118
1.3	1.5	2.759	1.030	1.518	2.119
1.3	1.6	2.815	1.037	1.502	2.120
1.3	1.7	2.874	1.043	1.486	2.121
1.3	1.8	2.935	1.050	1.471	2.122
1.3	1.9	2.998	1.057	1.455	2.123
1.3	2.0	3.063	1.064	1.440	2.124
1.4	1.0	2.588	1.010	1.569	2.115
1.4	1.1	2.621	1.014	1.559	2.116
1.4	1.2	2.662	1.019	1.545	2.117
1.4	1.3	2.711	1.024	1.531	2.118
1.4	1.4	2.764	1.030	1.515	2.120
1.4	1.5	2.822	1.037	1.499	2.121
1.4	1.6	2.883	1.044	1.482	2.122
1.4	1.7	2.947	1.051	1.465	2.123
1.4	1.8	3.013	1.058	1.450	2.124
1.4	1.9	3.081	1.065	1.434	2.125
1.4	2.0	3.151	1.073	1.419	2.126
1.5	1.0	2.630	1.015	1.555	2.116
1.5	1.1	2.668	1.019	1.543	2.118
1.5	1.2	2.716	1.024	1.528	2.119
1.5	1.3	2.770	1.031	1.512	2.121
1.5	1.4	2.829	1.037	1.496	2.122
1.5	1.5	2.892	1.044	1.479	2.123
1.5	1.6	2.958	1.051	1.462	2.125
1.5	1.7	3.027	1.059	1.445	2.126
1.5	1.8	3.098	1.066	1.429	2.127
1.5	1.9	3.171	1.074	1.413	2.128
1.5	2.0	3.245	1.082	1.397	2.129
1.6	1.0	2.677	1.020	1.540	2.118
1.6	1.1	2.722	1.025	1.526	2.120
1.6	1.2	2.775	1.031	1.510	2.121
1.6	1.3	2.834	1.037	1.493	2.123
1.6	1.4	2.899	1.044	1.476	2.125
1.6	1.5	2.967	1.052	1.458	2.126
1.6	1.6	3.039	1.059	1.441	2.128
1.6	1.7	3.113	1.067	1.423	2.129
1.6	1.8	3.189	1.075	1.407	2.130
1.6	1.9	3.267	1.083	1.390	2.132
1.6	2.0	3.346	1.091	1.374	2.133
1.7	1.0	2.729	1.026	1.524	2.120
1.7	1.1	2.779	1.031	1.508	2.122
1.7	1.2	2.839	1.037	1.491	2.124
1.7	1.3	2.904	1.044	1.473	2.126
1.7	1.4	2.974	1.052	1.455	2.128
1.7	1.5	3.047	1.060	1.437	2.129
1.7	1.6	3.124	1.068	1.419	2.131

1.7	1.7	3.204	1.076	1.402	2.132
1.7	1.8	3.285	1.084	1.384	2.134
1.7	1.9	3.368	1.092	1.368	2.135
1.7	2.0	3.453	1.101	1.352	2.137
1.8	1.0	2.785	1.031	1.506	2.123
1.8	1.1	2.842	1.037	1.490	2.125
1.8	1.2	2.907	1.044	1.472	2.127
1.8	1.3	2.978	1.052	1.453	2.129
1.8	1.4	3.053	1.059	1.434	2.131
1.8	1.5	3.132	1.068	1.415	2.133
1.8	1.6	3.215	1.076	1.397	2.134
1.8	1.7	3.300	1.085	1.379	2.136
1.8	1.8	3.386	1.093	1.362	2.138
1.8	1.9	3.475	1.102	1.345	2.139
1.8	2.0	3.565	1.111	1.329	2.141
1.9	1.0	2.844	1.038	1.489	2.125
1.9	1.1	2.908	1.044	1.471	2.127
1.9	1.2	2.978	1.051	1.452	2.130
1.9	1.3	3.055	1.059	1.432	2.132
1.9	1.4	3.137	1.067	1.413	2.134
1.9	1.5	3.222	1.076	1.394	2.136
1.9	1.6	3.310	1.085	1.375	2.138
1.9	1.7	3.400	1.093	1.357	2.140
1.9	1.8	3.492	1.102	1.340	2.142
1.9	1.9	3.586	1.111	1.323	2.143
1.9	2.0	3.681	1.120	1.307	2.145
2.0	1.0	2.908	1.044	1.470	2.128
2.0	1.1	2.977	1.051	1.451	2.130
2.0	1.2	3.054	1.059	1.432	2.133
2.0	1.3	3.137	1.067	1.412	2.135
2.0	1.4	3.224	1.075	1.392	2.138
2.0	1.5	3.315	1.084	1.372	2.140
2.0	1.6	3.408	1.093	1.354	2.142
2.0	1.7	3.504	1.102	1.335	2.144
2.0	1.8	3.602	1.112	1.318	2.146
2.0	1.9	3.702	1.121	1.301	2.148
2.0	2.0	3.803	1.130	1.285	2.149

A/B	B/C	CA/C0	CB/C0	CC/C0
1.00	1.0	1.0000	1.0000	1.0000
1.00	1.1	.986	.986	1.040
1.00	1.2	.983	.983	1.081
1.00	1.3	.988	.988	1.121
1.00	1.4	.998	.998	1.162
1.00	1.5	1.013	1.013	1.203
1.00	1.6	1.032	1.032	1.244
1.00	1.7	1.054	1.054	1.286
1.00	1.8	1.078	1.078	1.327
1.00	1.9	1.104	1.104	1.368
1.00	2.0	1.132	1.132	1.410
1.1	1.0	.964	1.025	1.025
1.1	1.1	.952	1.020	1.067
1.1	1.2	.950	1.026	1.110
1.1	1.3	.955	1.038	1.153
1.1	1.4	.966	1.056	1.196
1.1	1.5	.981	1.078	1.240
1.1	1.6	1.000	1.103	1.283
1.1	1.7	1.021	1.132	1.327
1.1	1.8	1.045	1.162	1.370
1.1	1.9	1.071	1.195	1.414
1.1	2.0	1.099	1.229	1.458
1.2	1.0	.934	1.058	1.058
1.2	1.1	.923	1.062	1.103
1.2	1.2	.922	1.075	1.148
1.2	1.3	.928	1.095	1.194
1.2	1.4	.939	1.120	1.240
1.2	1.5	.955	1.150	1.286
1.2	1.6	.973	1.182	1.332
1.2	1.7	.995	1.217	1.378
1.2	1.8	1.019	1.254	1.425
1.2	1.9	1.044	1.293	1.471
1.2	2.0	1.072	1.333	1.518
1.3	1.0	.909	1.097	1.097
1.3	1.1	.899	1.110	1.146
1.3	1.2	.899	1.131	1.194
1.3	1.3	.905	1.159	1.243
1.3	1.4	.917	1.191	1.292
1.3	1.5	.933	1.227	1.341
1.3	1.6	.951	1.266	1.390
1.3	1.7	.973	1.308	1.439
1.3	1.8	.997	1.351	1.488
1.3	1.9	1.022	1.397	1.538
1.3	2.0	1.049	1.443	1.587
1.4	1.0	.887	1.143	1.143
1.4	1.1	.879	1.164	1.194
1.4	1.2	.879	1.193	1.246
1.4	1.3	.886	1.228	1.298
1.4	1.4	.898	1.267	1.350
1.4	1.5	.914	1.310	1.402
1.4	1.6	.933	1.356	1.455
1.4	1.7	.954	1.404	1.507
1.4	1.8	.978	1.454	1.560
1.4	1.9	1.003	1.506	1.612
1.4	2.0	1.030	1.559	1.665
1.5	1.0	.869	1.193	1.193
1.5	1.1	.862	1.222	1.248
1.5	1.2	.862	1.259	1.304
1.5	1.3	.870	1.301	1.359
1.5	1.4	.882	1.348	1.415
1.5	1.5	.898	1.398	1.470
1.5	1.6	.917	1.451	1.526
1.5	1.7	.938	1.506	1.582
1.5	1.8	.961	1.563	1.638
1.5	1.9	.987	1.621	1.694
1.5	2.0	1.013	1.681	1.751
1.6	1.0	.853	1.248	1.248
1.6	1.1	.846	1.285	1.307
1.6	1.2	.848	1.330	1.366
1.6	1.3	.855	1.379	1.425
1.6	1.4	.868	1.433	1.485
1.6	1.5	.884	1.490	1.544
1.6	1.6	.903	1.550	1.604
1.6	1.7	.924	1.612	1.663
1.6	1.8	.947	1.676	1.723
1.6	1.9	.972	1.741	1.783
1.6	2.0	.999	1.807	1.843
1.7	1.0	.839	1.307	1.307
1.7	1.1	.833	1.352	1.370
1.7	1.2	.835	1.404	1.433
1.7	1.3	.843	1.461	1.496
1.7	1.4	.855	1.523	1.559
1.7	1.5	.871	1.587	1.623
1.7	1.6	.890	1.654	1.686

1.7	1.7	.912	1.723	1.750
1.7	1.8	.935	1.793	1.814
1.7	1.9	.960	1.865	1.877
1.7	2.0	.986	1.939	1.941
1.8	1.0	.827	1.370	1.370
1.8	1.1	.822	1.423	1.437
1.8	1.2	.824	1.483	1.504
1.8	1.3	.832	1.547	1.571
1.8	1.4	.845	1.616	1.639
1.8	1.5	.861	1.687	1.706
1.8	1.6	.880	1.762	1.774
1.8	1.7	.901	1.838	1.842
1.8	1.8	.924	1.915	1.913
1.8	1.9	.949	1.995	1.978
1.8	2.0	.975	2.075	2.046
1.9	1.0	.816	1.436	1.436
1.9	1.1	.811	1.497	1.507
1.9	1.2	.814	1.564	1.579
1.9	1.3	.822	1.637	1.650
1.9	1.4	.835	1.713	1.722
1.9	1.5	.851	1.792	1.794
1.9	1.6	.870	1.873	1.866
1.9	1.7	.892	1.957	1.938
1.9	1.8	.915	2.042	2.011
1.9	1.9	.939	2.128	2.083
1.9	2.0	.965	2.216	2.155
2.0	1.0	.807	1.505	1.505
2.0	1.1	.802	1.574	1.581
2.0	1.2	.805	1.650	1.657
2.0	1.3	.814	1.730	1.733
2.0	1.4	.826	1.813	1.810
2.0	1.5	.843	1.900	1.886
2.0	1.6	.862	1.989	1.963
2.0	1.7	.883	2.080	2.040
2.0	1.8	.906	2.172	2.116
2.0	1.9	.931	2.266	2.193
2.0	2.0	.957	2.361	2.270

A/B	B/C	RHOA/RHO0	RHOB/RHO0	RHOC/RHO0
1.0	1.0	1.000	1.000	1.000
1.0	1.1	1.013	1.013	.986
1.0	1.2	1.030	1.030	.983
1.0	1.3	1.050	1.050	.988
1.0	1.4	1.074	1.074	.998
1.0	1.5	1.100	1.100	1.013
1.0	1.6	1.128	1.128	1.032
1.0	1.7	1.158	1.158	1.054
1.0	1.8	1.189	1.189	1.078
1.0	1.9	1.222	1.222	1.104
1.0	2.0	1.256	1.256	1.132
1.1	1.0	1.025	.993	.993
1.1	1.1	1.043	1.006	.985
1.1	1.2	1.066	1.024	.986
1.1	1.3	1.092	1.045	.995
1.1	1.4	1.122	1.069	1.009
1.1	1.5	1.153	1.095	1.027
1.1	1.6	1.187	1.124	1.049
1.1	1.7	1.222	1.154	1.074
1.1	1.8	1.258	1.186	1.101
1.1	1.9	1.295	1.219	1.130
1.1	2.0	1.334	1.253	1.160
1.2	1.0	1.058	.992	.992
1.2	1.1	1.082	1.005	.988
1.2	1.2	1.111	1.023	.993
1.2	1.3	1.143	1.044	1.005
1.2	1.4	1.177	1.069	1.022
1.2	1.5	1.214	1.096	1.043
1.2	1.6	1.253	1.125	1.068
1.2	1.7	1.293	1.156	1.095
1.2	1.8	1.334	1.188	1.124
1.2	1.9	1.376	1.222	1.155
1.2	2.0	1.419	1.256	1.188
1.3	1.0	1.097	.994	.994
1.3	1.1	1.128	1.008	.994
1.3	1.2	1.162	1.026	1.002
1.3	1.3	1.199	1.048	1.017
1.3	1.4	1.239	1.072	1.036
1.3	1.5	1.281	1.100	1.060
1.3	1.6	1.325	1.130	1.086
1.3	1.7	1.370	1.161	1.116
1.3	1.8	1.417	1.194	1.147
1.3	1.9	1.464	1.228	1.180
1.3	2.0	1.512	1.263	1.215
1.4	1.0	1.143	.999	.999
1.4	1.1	1.179	1.013	1.002
1.4	1.2	1.219	1.031	1.012
1.4	1.3	1.262	1.053	1.029
1.4	1.4	1.307	1.079	1.051
1.4	1.5	1.355	1.107	1.077
1.4	1.6	1.404	1.137	1.105
1.4	1.7	1.454	1.168	1.136
1.4	1.8	1.505	1.202	1.169
1.4	1.9	1.558	1.237	1.204
1.4	2.0	1.611	1.272	1.240
1.5	1.0	1.193	1.006	1.006
1.5	1.1	1.235	1.020	1.011
1.5	1.2	1.281	1.038	1.024
1.5	1.3	1.330	1.061	1.043
1.5	1.4	1.381	1.086	1.066
1.5	1.5	1.433	1.115	1.093
1.5	1.6	1.488	1.145	1.123
1.5	1.7	1.543	1.178	1.156
1.5	1.8	1.600	1.212	1.190
1.5	1.9	1.657	1.247	1.227
1.5	2.0	1.715	1.283	1.264
1.6	1.0	1.248	1.014	1.014
1.6	1.1	1.296	1.028	1.021
1.6	1.2	1.348	1.046	1.035
1.6	1.3	1.402	1.069	1.056
1.6	1.4	1.458	1.095	1.081
1.6	1.5	1.517	1.124	1.109
1.6	1.6	1.576	1.155	1.141
1.6	1.7	1.637	1.188	1.175
1.6	1.8	1.699	1.223	1.210
1.6	1.9	1.762	1.258	1.248
1.6	2.0	1.825	1.295	1.287
1.7	1.0	1.307	1.022	1.022
1.7	1.1	1.361	1.036	1.031
1.7	1.2	1.418	1.055	1.047
1.7	1.3	1.479	1.078	1.069
1.7	1.4	1.541	1.105	1.095
1.7	1.5	1.605	1.134	1.125
1.7	1.6	1.670	1.165	1.158

1.7	1.7	1.736	1.199	1.192
1.7	1.8	1.803	1.234	1.229
1.7	1.9	1.871	1.270	1.268
1.7	2.0	1.940	1.308	1.307
1.8	1.0	1.370	1.032	1.032
1.8	1.1	1.430	1.045	1.042
1.8	1.2	1.493	1.065	1.059
1.8	1.3	1.559	1.088	1.082
1.8	1.4	1.627	1.115	1.109
1.8	1.5	1.697	1.144	1.140
1.8	1.6	1.768	1.176	1.173
1.8	1.7	1.840	1.210	1.209
1.8	1.8	1.913	1.246	1.247
1.8	1.9	1.986	1.283	1.286
1.8	2.0	2.060	1.321	1.327
1.9	1.0	1.436	1.041	1.041
1.9	1.1	1.502	1.055	1.052
1.9	1.2	1.572	1.074	1.071
1.9	1.3	1.644	1.098	1.095
1.9	1.4	1.718	1.125	1.123
1.9	1.5	1.793	1.155	1.154
1.9	1.6	1.870	1.187	1.188
1.9	1.7	1.948	1.221	1.225
1.9	1.8	2.026	1.257	1.263
1.9	1.9	2.105	1.295	1.303
1.9	2.0	2.185	1.334	1.345
2.0	1.0	1.505	1.050	1.050
2.0	1.1	1.577	1.064	1.063
2.0	1.2	1.653	1.084	1.082
2.0	1.3	1.731	1.107	1.107
2.0	1.4	1.812	1.135	1.135
2.0	1.5	1.893	1.165	1.168
2.0	1.6	1.976	1.198	1.203
2.0	1.7	2.059	1.233	1.240
2.0	1.8	2.144	1.269	1.279
2.0	1.9	2.229	1.307	1.320
2.0	2.0	2.314	1.346	1.362

A/B	B/C	DELTA(A)	DELTA(B)	DELTA(C)
1.0	1.0	2.500	2.500	2.500
1.0	1.1	2.541	2.541	2.410
1.0	1.2	2.568	2.568	2.336
1.0	1.3	2.582	2.582	2.274
1.0	1.4	2.588	2.588	2.222
1.0	1.5	2.586	2.586	2.178
1.0	1.6	2.579	2.579	2.139
1.0	1.7	2.568	2.568	2.105
1.0	1.8	2.555	2.555	2.075
1.0	1.9	2.539	2.539	2.048
1.0	2.0	2.522	2.522	2.024
1.1	1.0	2.601	2.446	2.446
1.1	1.1	2.648	2.470	2.362
1.1	1.2	2.679	2.481	2.292
1.1	1.3	2.697	2.482	2.234
1.1	1.4	2.706	2.475	2.185
1.1	1.5	2.707	2.464	2.143
1.1	1.6	2.702	2.449	2.106
1.1	1.7	2.694	2.431	2.074
1.1	1.8	2.682	2.412	2.046
1.1	1.9	2.667	2.392	2.020
1.1	2.0	2.651	2.371	1.998
1.2	1.0	2.704	2.387	2.387
1.2	1.1	2.757	2.397	2.308
1.2	1.2	2.793	2.395	2.242
1.2	1.3	2.815	2.385	2.188
1.2	1.4	2.827	2.370	2.141
1.2	1.5	2.831	2.351	2.102
1.2	1.6	2.829	2.330	2.067
1.2	1.7	2.822	2.308	2.037
1.2	1.8	2.812	2.285	2.010
1.2	1.9	2.799	2.261	1.987
1.2	2.0	2.784	2.238	1.966
1.3	1.0	2.809	2.326	2.326
1.3	1.1	2.868	2.323	2.251
1.3	1.2	2.909	2.311	2.190
1.3	1.3	2.936	2.293	2.139
1.3	1.4	2.951	2.272	2.095
1.3	1.5	2.958	2.248	2.058
1.3	1.6	2.959	2.223	2.025
1.3	1.7	2.954	2.197	1.997
1.3	1.8	2.945	2.172	1.972
1.3	1.9	2.934	2.147	1.950
1.3	2.0	2.920	2.122	1.930
1.4	1.0	2.916	2.264	2.264
1.4	1.1	2.981	2.252	2.194
1.4	1.2	3.028	2.232	2.136
1.4	1.3	3.059	2.208	2.088
1.4	1.4	3.078	2.181	2.047
1.4	1.5	3.088	2.154	2.012
1.4	1.6	3.091	2.126	1.982
1.4	1.7	3.089	2.099	1.955
1.4	1.8	3.082	2.072	1.932
1.4	1.9	3.072	2.046	1.911
1.4	2.0	3.060	2.021	1.892
1.5	1.0	3.026	2.203	2.203
1.5	1.1	3.097	2.183	2.137
1.5	1.2	3.149	2.157	2.083
1.5	1.3	3.185	2.128	2.038
1.5	1.4	3.208	2.098	2.000
1.5	1.5	3.222	2.068	1.967
1.5	1.6	3.227	2.039	1.938
1.5	1.7	3.227	2.010	1.913
1.5	1.8	3.222	1.983	1.891
1.5	1.9	3.214	1.956	1.871
1.5	2.0	3.204	1.931	1.854
1.6	1.0	3.137	2.144	2.144
1.6	1.1	3.215	2.117	2.082
1.6	1.2	3.273	2.087	2.031
1.6	1.3	3.313	2.055	1.989
1.6	1.4	3.341	2.023	1.953
1.6	1.5	3.358	1.991	1.922
1.6	1.6	3.366	1.960	1.895
1.6	1.7	3.369	1.931	1.871
1.6	1.8	3.366	1.903	1.851
1.6	1.9	3.360	1.877	1.832
1.6	2.0	3.351	1.852	1.816
1.7	1.0	3.251	2.087	2.087
1.7	1.1	3.336	2.055	2.029
1.7	1.2	3.399	2.021	1.981
1.7	1.3	3.445	1.987	1.941
1.7	1.4	3.476	1.953	1.907
1.7	1.5	3.497	1.920	1.878
1.7	1.6	3.509	1.889	1.853

1.7	1.7	3.514	1.860	1.831
1.7	1.8	3.513	1.832	1.811
1.7	1.9	3.509	1.806	1.794
1.7	2.0	3.501	1.781	1.779
1.8	1.0	3.366	2.033	2.033
1.8	1.1	3.459	1.997	1.978
1.8	1.2	3.528	1.960	1.933
1.8	1.3	3.579	1.924	1.895
1.8	1.4	3.615	1.889	1.863
1.8	1.5	3.639	1.856	1.836
1.8	1.6	3.654	1.825	1.812
1.8	1.7	3.662	1.796	1.792
1.8	1.8	3.664	1.768	1.773
1.8	1.9	3.661	1.742	1.757
1.8	2.0	3.655	1.718	1.743
1.9	1.0	3.484	1.981	1.981
1.9	1.1	3.584	1.942	1.929
1.9	1.2	3.660	1.904	1.887
1.9	1.3	3.716	1.867	1.851
1.9	1.4	3.757	1.831	1.821
1.9	1.5	3.785	1.798	1.796
1.9	1.6	3.803	1.767	1.773
1.9	1.7	3.813	1.738	1.754
1.9	1.8	3.818	1.710	1.737
1.9	1.9	3.817	1.685	1.722
1.9	2.0	3.813	1.662	1.708
2.0	1.0	3.604	1.932	1.932
2.0	1.1	3.712	1.891	1.883
2.0	1.2	3.794	1.851	1.843
2.0	1.3	3.856	1.814	1.810
2.0	1.4	3.901	1.778	1.781
2.0	1.5	3.933	1.745	1.757
2.0	1.6	3.955	1.714	1.736
2.0	1.7	3.968	1.685	1.718
2.0	1.8	3.975	1.658	1.702
2.0	1.9	3.977	1.634	1.688
2.0	2.0	3.975	1.611	1.675

A/B	B/C	GAMMA(A)	GAMMA(B)	GAMMA(C)
1.0	1.0	1.000	1.000	1.000
1.0	1.1	.990	.990	1.016
1.0	1.2	.980	.980	1.026
1.0	1.3	.970	.970	1.031
1.0	1.4	.959	.959	1.032
1.0	1.5	.949	.949	1.031
1.0	1.6	.939	.939	1.027
1.0	1.7	.929	.929	1.021
1.0	1.8	.919	.919	1.015
1.0	1.9	.910	.910	1.008
1.0	2.0	.901	.901	1.000
1.1	1.0	.978	1.009	1.009
1.1	1.1	.966	1.001	1.023
1.1	1.2	.953	.993	1.030
1.1	1.3	.941	.984	1.033
1.1	1.4	.929	.974	1.032
1.1	1.5	.917	.965	1.029
1.1	1.6	.905	.956	1.024
1.1	1.7	.894	.947	1.017
1.1	1.8	.884	.937	1.010
1.1	1.9	.874	.929	1.002
1.1	2.0	.864	.920	.994
1.2	1.0	.954	1.017	1.017
1.2	1.1	.939	1.011	1.029
1.2	1.2	.925	1.004	1.034
1.2	1.3	.911	.996	1.036
1.2	1.4	.897	.988	1.034
1.2	1.5	.885	.980	1.029
1.2	1.6	.872	.971	1.023
1.2	1.7	.861	.963	1.016
1.2	1.8	.850	.954	1.008
1.2	1.9	.840	.946	1.000
1.2	2.0	.830	.938	.991
1.3	1.0	.928	1.025	1.025
1.3	1.1	.912	1.020	1.035
1.3	1.2	.896	1.015	1.039
1.3	1.3	.881	1.008	1.039
1.3	1.4	.867	1.001	1.036
1.3	1.5	.853	.994	1.031
1.3	1.6	.840	.986	1.025
1.3	1.7	.829	.978	1.018
1.3	1.8	.817	.970	1.009
1.3	1.9	.807	.962	1.001
1.3	2.0	.797	.954	.992
1.4	1.0	.902	1.032	1.032
1.4	1.1	.884	1.029	1.041
1.4	1.2	.867	1.025	1.044
1.4	1.3	.851	1.020	1.044
1.4	1.4	.837	1.014	1.041
1.4	1.5	.823	1.007	1.035
1.4	1.6	.810	1.000	1.029
1.4	1.7	.798	.993	1.021
1.4	1.8	.787	.986	1.013
1.4	1.9	.777	.978	1.005
1.4	2.0	.767	.971	.996
1.5	1.0	.876	1.039	1.039
1.5	1.1	.857	1.038	1.047
1.5	1.2	.839	1.036	1.050
1.5	1.3	.823	1.032	1.050
1.5	1.4	.808	1.027	1.046
1.5	1.5	.794	1.021	1.041
1.5	1.6	.781	1.015	1.035
1.5	1.7	.769	1.008	1.027
1.5	1.8	.758	1.001	1.019
1.5	1.9	.748	.994	1.011
1.5	2.0	.739	.987	1.002
1.6	1.0	.850	1.047	1.047
1.6	1.1	.831	1.048	1.055
1.6	1.2	.813	1.047	1.058
1.6	1.3	.796	1.044	1.057
1.6	1.4	.781	1.040	1.054
1.6	1.5	.767	1.035	1.048
1.6	1.6	.754	1.029	1.042
1.6	1.7	.742	1.023	1.035
1.6	1.8	.731	1.017	1.027
1.6	1.9	.721	1.010	1.019
1.6	2.0	.712	1.003	1.010
1.7	1.0	.825	1.055	1.055
1.7	1.1	.805	1.058	1.063
1.7	1.2	.787	1.058	1.066
1.7	1.3	.770	1.056	1.065
1.7	1.4	.755	1.053	1.062
1.7	1.5	.741	1.049	1.057
1.7	1.6	.729	1.044	1.051

1.7	1.7	.717	1.038	1.044
1.7	1.8	.706	1.032	1.036
1.7	1.9	.697	1.026	1.029
1.7	2.0	.688	1.020	1.020
1.8	1.0	.801	1.064	1.064
1.8	1.1	.781	1.068	1.072
1.8	1.2	.763	1.070	1.075
1.8	1.3	.746	1.069	1.075
1.8	1.4	.731	1.067	1.072
1.8	1.5	.717	1.064	1.068
1.8	1.6	.705	1.059	1.062
1.8	1.7	.693	1.054	1.055
1.8	1.8	.683	1.049	1.048
1.8	1.9	.674	1.043	1.040
1.8	2.0	.665	1.037	1.032
1.9	1.0	.778	1.073	1.073
1.9	1.1	.758	1.079	1.081
1.9	1.2	.739	1.082	1.085
1.9	1.3	.723	1.082	1.085
1.9	1.4	.708	1.081	1.083
1.9	1.5	.695	1.079	1.079
1.9	1.6	.682	1.075	1.074
1.9	1.7	.671	1.070	1.067
1.9	1.8	.661	1.065	1.060
1.9	1.9	.652	1.060	1.053
1.9	2.0	.643	1.054	1.045
2.0	1.0	.756	1.083	1.083
2.0	1.1	.736	1.090	1.092
2.0	1.2	.717	1.095	1.096
2.0	1.3	.701	1.096	1.097
2.0	1.4	.687	1.096	1.095
2.0	1.5	.673	1.094	1.092
2.0	1.6	.661	1.091	1.087
2.0	1.7	.651	1.087	1.081
2.0	1.8	.641	1.083	1.074
2.0	1.9	.632	1.078	1.067
2.0	2.0	.624	1.072	1.060

A/B	B/C	MU(A)	MU(B)	MU(C)
1.0	1.0	1.000	1.000	1.000
1.0	1.1	.995	.995	1.012
1.0	1.2	.991	.991	1.023
1.0	1.3	.990	.990	1.033
1.0	1.4	.989	.989	1.041
1.0	1.5	.990	.990	1.048
1.0	1.6	.991	.991	1.055
1.0	1.7	.993	.993	1.061
1.0	1.8	.995	.995	1.067
1.0	1.9	.998	.998	1.072
1.0	2.0	1.000	1.000	1.076
1.1	1.0	.987	1.007	1.007
1.1	1.1	.981	1.004	1.019
1.1	1.2	.978	1.003	1.030
1.1	1.3	.976	1.003	1.039
1.1	1.4	.975	1.005	1.047
1.1	1.5	.975	1.007	1.055
1.1	1.6	.976	1.009	1.061
1.1	1.7	.978	1.012	1.067
1.1	1.8	.980	1.015	1.072
1.1	1.9	.982	1.018	1.077
1.1	2.0	.984	1.022	1.081
1.2	1.0	.975	1.016	1.016
1.2	1.1	.969	1.015	1.028
1.2	1.2	.965	1.015	1.038
1.2	1.3	.963	1.017	1.047
1.2	1.4	.962	1.020	1.055
1.2	1.5	.962	1.023	1.062
1.2	1.6	.962	1.027	1.068
1.2	1.7	.963	1.030	1.074
1.2	1.8	.965	1.034	1.079
1.2	1.9	.967	1.038	1.084
1.2	2.0	.969	1.042	1.088
1.3	1.0	.963	1.025	1.025
1.3	1.1	.956	1.026	1.037
1.3	1.2	.952	1.028	1.047
1.3	1.3	.950	1.031	1.056
1.3	1.4	.949	1.035	1.063
1.3	1.5	.948	1.039	1.070
1.3	1.6	.949	1.044	1.077
1.3	1.7	.950	1.048	1.082
1.3	1.8	.951	1.053	1.087
1.3	1.9	.953	1.057	1.092
1.3	2.0	.955	1.062	1.096
1.4	1.0	.951	1.035	1.035
1.4	1.1	.945	1.037	1.046
1.4	1.2	.940	1.041	1.056
1.4	1.3	.938	1.045	1.065
1.4	1.4	.936	1.050	1.073
1.4	1.5	.936	1.055	1.080
1.4	1.6	.936	1.060	1.086
1.4	1.7	.937	1.066	1.091
1.4	1.8	.938	1.071	1.096
1.4	1.9	.939	1.076	1.101
1.4	2.0	.941	1.081	1.105
1.5	1.0	.940	1.045	1.045
1.5	1.1	.934	1.049	1.056
1.5	1.2	.929	1.054	1.066
1.5	1.3	.926	1.059	1.075
1.5	1.4	.925	1.065	1.082
1.5	1.5	.924	1.071	1.089
1.5	1.6	.924	1.077	1.095
1.5	1.7	.924	1.082	1.101
1.5	1.8	.925	1.088	1.105
1.5	1.9	.927	1.094	1.110
1.5	2.0	.928	1.099	1.114
1.6	1.0	.930	1.056	1.056
1.6	1.1	.923	1.061	1.067
1.6	1.2	.918	1.067	1.076
1.6	1.3	.915	1.073	1.085
1.6	1.4	.913	1.080	1.092
1.6	1.5	.912	1.086	1.099
1.6	1.6	.912	1.092	1.105
1.6	1.7	.913	1.099	1.110
1.6	1.8	.913	1.105	1.115
1.6	1.9	.915	1.111	1.119
1.6	2.0	.916	1.116	1.123
1.7	1.0	.920	1.066	1.066
1.7	1.1	.913	1.073	1.077
1.7	1.2	.908	1.080	1.087
1.7	1.3	.905	1.087	1.095
1.7	1.4	.903	1.094	1.103
1.7	1.5	.901	1.101	1.109
1.7	1.6	.901	1.108	1.115

1.7	1.7	.901	1.114	1.120
1.7	1.8	.902	1.121	1.125
1.7	1.9	.903	1.127	1.129
1.7	2.0	.904	1.133	1.133
1.8	1.0	.910	1.077	1.077
1.8	1.1	.903	1.084	1.088
1.8	1.2	.898	1.092	1.097
1.8	1.3	.894	1.100	1.105
1.8	1.4	.892	1.108	1.113
1.8	1.5	.891	1.115	1.119
1.8	1.6	.890	1.122	1.125
1.8	1.7	.891	1.129	1.130
1.8	1.8	.891	1.136	1.135
1.8	1.9	.892	1.142	1.139
1.8	2.0	.893	1.149	1.143
1.9	1.0	.901	1.087	1.087
1.9	1.1	.893	1.096	1.098
1.9	1.2	.888	1.104	1.108
1.9	1.3	.885	1.113	1.116
1.9	1.4	.882	1.121	1.123
1.9	1.5	.881	1.129	1.129
1.9	1.6	.880	1.137	1.135
1.9	1.7	.880	1.144	1.140
1.9	1.8	.881	1.151	1.145
1.9	1.9	.881	1.157	1.149
1.9	2.0	.882	1.164	1.153
2.0	1.0	.892	1.098	1.098
2.0	1.1	.884	1.107	1.109
2.0	1.2	.879	1.116	1.118
2.0	1.3	.875	1.125	1.126
2.0	1.4	.873	1.134	1.133
2.0	1.5	.871	1.142	1.140
2.0	1.6	.870	1.150	1.145
2.0	1.7	.870	1.158	1.150
2.0	1.8	.870	1.165	1.155
2.0	1.9	.871	1.172	1.159
2.0	2.0	.872	1.178	1.163

A/B	B/C	THETA+	THETA-	TAU/TAU0	PSI
1.0	1.0	.167	.167	1.000	1.000
1.0	1.1	.169	.163	1.004	1.000
1.0	1.2	.170	.159	1.014	.998
1.0	1.3	.169	.155	1.029	.997
1.0	1.4	.167	.151	1.047	.995
1.0	1.5	.165	.147	1.069	.992
1.0	1.6	.162	.143	1.094	.989
1.0	1.7	.158	.139	1.121	.986
1.0	1.8	.155	.135	1.150	.983
1.0	1.9	.151	.132	1.180	.980
1.0	2.0	.147	.128	1.211	.977
1.1	1.0	.170	.163	1.004	1.000
1.1	1.1	.170	.159	1.011	.999
1.1	1.2	.170	.155	1.024	.997
1.1	1.3	.169	.151	1.042	.995
1.1	1.4	.166	.147	1.064	.993
1.1	1.5	.163	.143	1.089	.990
1.1	1.6	.160	.139	1.117	.987
1.1	1.7	.156	.134	1.147	.984
1.1	1.8	.152	.131	1.178	.981
1.1	1.9	.149	.127	1.211	.978
1.1	2.0	.145	.123	1.245	.975
1.2	1.0	.172	.158	1.013	.999
1.2	1.1	.172	.154	1.023	.998
1.2	1.2	.171	.150	1.040	.996
1.2	1.3	.169	.145	1.061	.994
1.2	1.4	.166	.141	1.085	.991
1.2	1.5	.163	.137	1.113	.988
1.2	1.6	.159	.132	1.143	.985
1.2	1.7	.155	.128	1.175	.982
1.2	1.8	.152	.124	1.209	.979
1.2	1.9	.148	.120	1.244	.976
1.2	2.0	.144	.117	1.281	.972
1.3	1.0	.173	.152	1.026	.998
1.3	1.1	.173	.148	1.040	.996
1.3	1.2	.172	.143	1.059	.994
1.3	1.3	.169	.139	1.082	.992
1.3	1.4	.166	.134	1.109	.989
1.3	1.5	.163	.130	1.139	.986
1.3	1.6	.159	.125	1.172	.983
1.3	1.7	.155	.121	1.206	.980
1.3	1.8	.151	.117	1.242	.977
1.3	1.9	.147	.114	1.279	.974
1.3	2.0	.143	.110	1.318	.971
1.4	1.0	.174	.146	1.043	.996
1.4	1.1	.174	.141	1.059	.995
1.4	1.2	.172	.137	1.080	.993
1.4	1.3	.170	.132	1.106	.991
1.4	1.4	.166	.127	1.135	.988
1.4	1.5	.163	.123	1.167	.985
1.4	1.6	.159	.119	1.201	.982
1.4	1.7	.155	.114	1.238	.979
1.4	1.8	.151	.111	1.276	.976
1.4	1.9	.147	.107	1.315	.972
1.4	2.0	.143	.103	1.356	.969
1.5	1.0	.174	.140	1.061	.995
1.5	1.1	.174	.135	1.079	.994
1.5	1.2	.172	.130	1.103	.992
1.5	1.3	.170	.125	1.130	.989
1.5	1.4	.166	.121	1.161	.987
1.5	1.5	.163	.116	1.195	.984
1.5	1.6	.159	.112	1.232	.981
1.5	1.7	.155	.108	1.270	.978
1.5	1.8	.150	.104	1.310	.975
1.5	1.9	.146	.101	1.351	.972
1.5	2.0	.142	.097	1.393	.969
1.6	1.0	.175	.134	1.081	.994
1.6	1.1	.174	.129	1.101	.993
1.6	1.2	.172	.124	1.126	.991
1.6	1.3	.170	.119	1.156	.988
1.6	1.4	.166	.114	1.189	.986
1.6	1.5	.162	.110	1.224	.983
1.6	1.6	.158	.106	1.262	.980
1.6	1.7	.154	.102	1.302	.977
1.6	1.8	.150	.098	1.344	.974
1.6	1.9	.146	.095	1.386	.971
1.6	2.0	.142	.091	1.430	.969
1.7	1.0	.175	.127	1.102	.993
1.7	1.1	.174	.122	1.124	.992
1.7	1.2	.172	.117	1.151	.990
1.7	1.3	.169	.113	1.182	.988
1.7	1.4	.166	.108	1.216	.985
1.7	1.5	.162	.104	1.253	.983
1.7	1.6	.158	.100	1.293	.980

1.7	1.7	.154	.096	1.334	.977
1.7	1.8	.150	.092	1.377	.974
1.7	1.9	.145	.089	1.422	.972
1.7	2.0	.141	.086	1.467	.969
1.8	1.0	.175	.122	1.124	.992
1.8	1.1	.174	.117	1.147	.991
1.8	1.2	.172	.112	1.175	.990
1.8	1.3	.169	.107	1.207	.988
1.8	1.4	.166	.102	1.243	.985
1.8	1.5	.162	.098	1.282	.983
1.8	1.6	.158	.094	1.323	.980
1.8	1.7	.154	.091	1.366	.978
1.8	1.8	.149	.087	1.410	.975
1.8	1.9	.145	.084	1.456	.972
1.8	2.0	.141	.081	1.503	.970
1.9	1.0	.175	.116	1.146	.992
1.9	1.1	.174	.111	1.170	.991
1.9	1.2	.172	.106	1.199	.989
1.9	1.3	.169	.101	1.233	.988
1.9	1.4	.165	.097	1.270	.986
1.9	1.5	.162	.093	1.310	.983
1.9	1.6	.157	.089	1.352	.981
1.9	1.7	.153	.086	1.396	.978
1.9	1.8	.149	.082	1.442	.976
1.9	1.9	.145	.079	1.489	.973
1.9	2.0	.141	.076	1.538	.971
2.0	1.0	.175	.111	1.168	.991
2.0	1.1	.174	.106	1.193	.991
2.0	1.2	.172	.101	1.224	.990
2.0	1.3	.169	.096	1.258	.988
2.0	1.4	.165	.092	1.296	.986
2.0	1.5	.161	.088	1.337	.984
2.0	1.6	.157	.084	1.381	.982
2.0	1.7	.153	.081	1.426	.979
2.0	1.8	.149	.078	1.473	.977
2.0	1.9	.144	.075	1.522	.975
2.0	2.0	.140	.072	1.571	.972

A/B	B/C	DELTA+	DELTA-
1.0	1.0	2.500	2.500
1.0	1.1	2.541	2.454
1.0	1.2	2.568	2.413
1.0	1.3	2.582	2.377
1.0	1.4	2.588	2.344
1.0	1.5	2.586	2.314
1.0	1.6	2.579	2.286
1.0	1.7	2.568	2.259
1.0	1.8	2.555	2.235
1.0	1.9	2.539	2.212
1.0	2.0	2.522	2.190
1.1	1.0	2.549	2.446
1.1	1.1	2.577	2.410
1.1	1.2	2.596	2.372
1.1	1.3	2.605	2.337
1.1	1.4	2.606	2.305
1.1	1.5	2.601	2.274
1.1	1.6	2.592	2.246
1.1	1.7	2.579	2.220
1.1	1.8	2.564	2.195
1.1	1.9	2.547	2.172
1.1	2.0	2.529	2.151
1.2	1.0	2.599	2.387
1.2	1.1	2.624	2.350
1.2	1.2	2.641	2.313
1.2	1.3	2.648	2.277
1.2	1.4	2.648	2.245
1.2	1.5	2.642	2.214
1.2	1.6	2.632	2.185
1.2	1.7	2.619	2.159
1.2	1.8	2.604	2.134
1.2	1.9	2.587	2.111
1.2	2.0	2.570	2.089
1.3	1.0	2.648	2.326
1.3	1.1	2.675	2.286
1.3	1.2	2.692	2.248
1.3	1.3	2.700	2.212
1.3	1.4	2.700	2.178
1.3	1.5	2.695	2.147
1.3	1.6	2.686	2.118
1.3	1.7	2.674	2.091
1.3	1.8	2.660	2.066
1.3	1.9	2.644	2.043
1.3	2.0	2.627	2.021
1.4	1.0	2.699	2.264
1.4	1.1	2.729	2.222
1.4	1.2	2.748	2.183
1.4	1.3	2.757	2.146
1.4	1.4	2.759	2.112
1.4	1.5	2.756	2.081
1.4	1.6	2.748	2.051
1.4	1.7	2.737	2.024
1.4	1.8	2.724	1.999
1.4	1.9	2.710	1.976
1.4	2.0	2.694	1.954
1.5	1.0	2.752	2.203
1.5	1.1	2.785	2.160
1.5	1.2	2.807	2.119
1.5	1.3	2.818	2.082
1.5	1.4	2.823	2.048
1.5	1.5	2.821	2.016
1.5	1.6	2.815	1.987
1.5	1.7	2.806	1.961
1.5	1.8	2.795	1.936
1.5	1.9	2.781	1.913
1.5	2.0	2.767	1.892
1.6	1.0	2.806	2.144
1.6	1.1	2.844	2.100
1.6	1.2	2.868	2.059
1.6	1.3	2.883	2.021
1.6	1.4	2.890	1.987
1.6	1.5	2.891	1.956
1.6	1.6	2.887	1.927
1.6	1.7	2.880	1.901
1.6	1.8	2.870	1.877
1.6	1.9	2.858	1.854
1.6	2.0	2.845	1.834
1.7	1.0	2.863	2.087
1.7	1.1	2.905	2.042
1.7	1.2	2.933	2.001
1.7	1.3	2.951	1.964
1.7	1.4	2.961	1.930
1.7	1.5	2.965	1.899
1.7	1.6	2.963	1.871

1.7	1.7	2.958	1.845
1.7	1.8	2.949	1.822
1.7	1.9	2.939	1.800
1.7	2.0	2.927	1.780
1.8	1.0	2.922	2.033
1.8	1.1	2.968	1.987
1.8	1.2	3.001	1.946
1.8	1.3	3.023	1.910
1.8	1.4	3.036	1.876
1.8	1.5	3.042	1.846
1.8	1.6	3.042	1.819
1.8	1.7	3.039	1.794
1.8	1.8	3.033	1.771
1.8	1.9	3.024	1.750
1.8	2.0	3.014	1.730
1.9	1.0	2.983	1.981
1.9	1.1	3.035	1.936
1.9	1.2	3.071	1.895
1.9	1.3	3.097	1.859
1.9	1.4	3.113	1.826
1.9	1.5	3.122	1.797
1.9	1.6	3.125	1.770
1.9	1.7	3.124	1.746
1.9	1.8	3.120	1.724
1.9	1.9	3.113	1.703
1.9	2.0	3.104	1.685
2.0	1.0	3.047	1.932
2.0	1.1	3.103	1.887
2.0	1.2	3.145	1.847
2.0	1.3	3.174	1.812
2.0	1.4	3.194	1.780
2.0	1.5	3.206	1.751
2.0	1.6	3.212	1.725
2.0	1.7	3.213	1.702
2.0	1.8	3.210	1.680
2.0	1.9	3.205	1.661
2.0	2.0	3.198	1.643

A/B	B/C	GAMMA+	GAMMA-
1.0	1.0	1.000	1.000
1.0	1.1	1.016	.981
1.0	1.2	1.026	.965
1.0	1.3	1.031	.949
1.0	1.4	1.032	.935
1.0	1.5	1.031	.922
1.0	1.6	1.027	.910
1.0	1.7	1.021	.898
1.0	1.8	1.015	.888
1.0	1.9	1.008	.878
1.0	2.0	1.000	.868
1.1	1.0	1.020	.978
1.1	1.1	1.030	.963
1.1	1.2	1.037	.947
1.1	1.3	1.039	.932
1.1	1.4	1.039	.918
1.1	1.5	1.035	.905
1.1	1.6	1.030	.893
1.1	1.7	1.024	.881
1.1	1.8	1.017	.871
1.1	1.9	1.009	.861
1.1	2.0	1.001	.851
1.2	1.0	1.038	.954
1.2	1.1	1.048	.938
1.2	1.2	1.053	.922
1.2	1.3	1.055	.907
1.2	1.4	1.053	.893
1.2	1.5	1.050	.880
1.2	1.6	1.044	.867
1.2	1.7	1.038	.855
1.2	1.8	1.030	.844
1.2	1.9	1.023	.834
1.2	2.0	1.015	.825
1.3	1.0	1.057	.928
1.3	1.1	1.066	.911
1.3	1.2	1.072	.895
1.3	1.3	1.073	.879
1.3	1.4	1.072	.865
1.3	1.5	1.068	.851
1.3	1.6	1.063	.838
1.3	1.7	1.057	.826
1.3	1.8	1.049	.815
1.3	1.9	1.042	.805
1.3	2.0	1.034	.795
1.4	1.0	1.075	.902
1.4	1.1	1.085	.884
1.4	1.2	1.091	.867
1.4	1.3	1.093	.851
1.4	1.4	1.092	.836
1.4	1.5	1.089	.822
1.4	1.6	1.084	.809
1.4	1.7	1.078	.797
1.4	1.8	1.071	.786
1.4	1.9	1.064	.776
1.4	2.0	1.056	.766
1.5	1.0	1.094	.876
1.5	1.1	1.105	.857
1.5	1.2	1.111	.839
1.5	1.3	1.114	.823
1.5	1.4	1.113	.808
1.5	1.5	1.111	.794
1.5	1.6	1.106	.781
1.5	1.7	1.101	.769
1.5	1.8	1.094	.758
1.5	1.9	1.087	.748
1.5	2.0	1.080	.738
1.6	1.0	1.113	.850
1.6	1.1	1.125	.831
1.6	1.2	1.132	.812
1.6	1.3	1.135	.796
1.6	1.4	1.136	.781
1.6	1.5	1.133	.767
1.6	1.6	1.130	.754
1.6	1.7	1.125	.742
1.6	1.8	1.119	.731
1.6	1.9	1.112	.721
1.6	2.0	1.105	.712
1.7	1.0	1.132	.825
1.7	1.1	1.145	.805
1.7	1.2	1.154	.787
1.7	1.3	1.158	.770
1.7	1.4	1.159	.755
1.7	1.5	1.157	.741
1.7	1.6	1.154	.729

1.7	1.7	1.149	.717
1.7	1.8	1.144	.706
1.7	1.9	1.138	.697
1.7	2.0	1.131	.688
1.8	1.0	1.151	.801
1.8	1.1	1.166	.781
1.8	1.2	1.176	.762
1.8	1.3	1.181	.746
1.8	1.4	1.182	.731
1.8	1.5	1.182	.717
1.8	1.6	1.179	.705
1.8	1.7	1.175	.693
1.8	1.8	1.170	.683
1.8	1.9	1.164	.674
1.8	2.0	1.158	.665
1.9	1.0	1.172	.778
1.9	1.1	1.188	.758
1.9	1.2	1.198	.739
1.9	1.3	1.204	.723
1.9	1.4	1.207	.708
1.9	1.5	1.207	.695
1.9	1.6	1.205	.682
1.9	1.7	1.201	.671
1.9	1.8	1.197	.661
1.9	1.9	1.191	.652
1.9	2.0	1.185	.643
2.0	1.0	1.192	.756
2.0	1.1	1.210	.736
2.0	1.2	1.221	.717
2.0	1.3	1.229	.701
2.0	1.4	1.232	.687
2.0	1.5	1.233	.673
2.0	1.6	1.231	.661
2.0	1.7	1.229	.651
2.0	1.8	1.224	.641
2.0	1.9	1.219	.632
2.0	2.0	1.214	.624

Program 3

```

C *****
C THIS PROGRAM PRODUCES A CONTOUR MAP OF THE VISCOSITY
C INCREMENT OVER THE AXIAL RANGE A/B, B/C 1.0 TO 3.0, IN
C STEPS OF 0.5 OF THE FUNCTION FROM NU=2.5 TO NU=7.0
C *****

```

```

PROGRAM MAIN(INPUT,OUTPUT,TAPE2=INPUT,TAPE3=OUTPUT)
COMMON/PARAM/A,C,NN

```

```
EXTERNAL FUN
```

```
DIMENSION ALPHA(10,21,21),NU(21,21),H(10)
```

```
REAL NU
```

```
NN=0
```

```
COMPUTE THE ELLIPTIC INTEGRALS
```

```
DO45 K=1,10
```

```
A=0.9
```

```
NN=NN+1
```

```
DO40 I=1,21
```

```
A=A+0.1
```

```
C=1.0/0.9
```

```
DO30 N=1,21
```

```
C=C/(1.0+0.1*C)
```

```
SET LIMITS FOR NUMERICAL INTEGRATION (THESE LIMITS
BELOW HAVE BEEN PREVIOUSLY TESTED FOR CONVERGENCE)
```

```
AA=0.0
```

```
BB=1000000
```

```
IF(NN.EQ.10)BB=500000000
```

```
MAXDIV=50
```

```
EPS=1.0E-08
```

```
ACC=0.0
```

```
IFAIL=0
```

```
CALL U.K. "NAG" LIBRARY ROUTINE FOR NUMERICAL EVALUATION
OF THE INTEGRALS "ALPHA" GIVEN IN THE SUBROUTINE BELOW
```

```
CALL DO1AGF(AA,BB,FUN,MAXDIV,EPS,ACC,ANS,ERROR,NOFUN,IFAIL)
```

```
ALPHA(NN,I,N)=ANS
```

```
30 CONTINUE
```

```
40 CONTINUE
```

```
45 CONTINUE
```

```
B=1.0
```

```
A=0.9
```

```
DO80 J=1,21
```

```
A=A+0.1
```

```
C=1.0/0.9
```

```
DO70 N=1,21
```

```
C=C/(1.0+0.1*C)
```

```
NOW COMPUTE THE FUNCTION VALUES USING THE STORED INTEGRAL VALUES
```

```
NU(J,N)=(1.0/(A*B*C))*(((4.0/15.0)*((ALPHA(7,J,N)+ALPHA(3,J,N)
```

```
+ ALPHA(9,J,N))/(ALPHA(8,J,N)*ALPHA(9,J,N)+ALPHA(9,J,N)*ALPHA
```

```
+ (7,J,N)+ALPHA(7,J,N)*ALPHA(8,J,N)))+(1.0/5.0)*(((ALPHA(2,J,N)
```

```
+ ALPHA(3,J,N))/(ALPHA(4,J,N)*(B*B*ALPHA(2,J,N)+C*C*ALPHA(3,J,N)
```

```
+ )))+(ALPHA(3,J,N)+ALPHA(1,J,N))/(ALPHA(5,J,N)*(C*C*ALPHA(3,J,N)
```

```
+ A*A*ALPHA(1,J,N)))+(ALPHA(1,J,N)+ALPHA(2,J,N))/(ALPHA(6,J,N)
```

```
+ (A*A*ALPHA(1,J,N)+B*B*ALPHA(2,J,N))))
```

```
70 CONTINUE
```

```
80 CONTINUE
```

```
CALL CONTOUR PLOTTING ROUTINE
```

```
CALL PAPER(1)
```

```
H(1)=2.5
```

```
H(2)=3.0
```

```
H(3)=3.5
```

```
H(4)=4.0
```

```
H(5)=4.5
```

```
H(6)=5.0
```

```
H(7)=5.5
```

```
H(8)=6.0
```

```
H(9)=6.5
```

```
H(10)=7.0
```

```
CALL MAP(1.0,3.0,1.0,3.0)
```

```
CALL SCALES
```

```
CALL BORDER
```

```
CALL CONTRL(NU,1,21,21,1,21,21,H,1,10)
```

```
CALL GREND
```

```
STOP
```

```
END
```

C
C
C

```

REAL FUNCTION FUN(X)
COMMON/PARAM/A,C,NN
B=1.0
GOTO(10,20,30,40,50,60,70,80,90,100),NN
10 FUN=1/((A*A+X)**1.5*(B*B+X)**0.5*(C*C+X)**0.5)
   RETURN
20 FUN=1/((A*A+X)**0.5*(B*B+X)**1.5*(C*C+X)**0.5)
   RETURN
30 FUN=1/((A*A+X)**0.5*(B*B+X)**0.5*(C*C+X)**1.5)
   RETURN
40 FUN=1/((A*A+X)**0.5*(B*B+X)**1.5*(C*C+X)**1.5)
   RETURN
50 FUN=1/((A*A+X)**1.5*(B*B+X)**0.5*(C*C+X)**1.5)
   RETURN
60 FUN=1/((A*A+X)**1.5*(B*B+X)**1.5*(C*C+X)**0.5)
   RETURN
70 FUN=X/((A*A+X)**0.5*(B*B+X)**1.5*(C*C+X)**1.5)
   RETURN
80 FUN=X/((A*A+X)**1.5*(B*B+X)**0.5*(C*C+X)**1.5)
   RETURN
90 FUN=X/((A*A+X)**1.5*(B*B+X)**1.5*(C*C+X)**0.5)
   RETURN
100 FUN=1.0/(((A*A+X)*(B*B+X)*(C*C+X))**0.5)
    RETURN
    END

```

```

*****
THIS PROGRAM GIVES PLOTS OF THE LINE SOLUTIONS OF THE
VARIOUS TRIAXIAL SHAPE FUNCTIONS ( AS TABULATED IN THE
PREVIOUS PROGRAM) FOR AXIAL RATIOS A/B = B/C = 1.5, IN
ORDER TO DETERMINE THE BEST COMBINATION FOR PRODUCING
A UNIQUE SOLUTION.
*****

```

```

PROGRAM MAIN(INPUT,OUTPUT,TAPE2=INPUT,TAPE3=OUTPUT)
COMMON/PARAM/A,C,NN
EXTERNAL FUN
DIMENSION ALPHA(10,21,21),NU(21,21),F(21,21),R(21,21),H(1)
+ ,BETA(21,21),CA(21,21),CB(21,21),CC(21,21),M(21,21),O(21,21)
+ ,P(21,21),TPLS(21,21),TMNS(21,21),RHOA(21,21),RHOB(21,21)
+ ,RHOC(21,21),TAU(21,21),PSI(21,21),DELA(21,21),DELB(21,21)
+ ,DELC(21,21),GAMMAA(21,21),GAMMAB(21,21),GAMMAC(21,21),MUA(21,21)
+ ,MUB(21,21),MUC(21,21),DPLS(21,21),DMNS(21,21),GPLS(21,21)
+ ,GMNS(21,21),V(21,21)
+ ,X1(21,21),X2(21,21),X3(21,21),X4(21,21),X5(21,21)
+ ,T1(21,21),T2(21,21),T3(21,21),T4(21,21),T5(21,21)
REAL NU,M,O,P,MUA,MUB,MUC,PSI
COMPUTE THE ELLIPTIC INTEGRALS
NN=0
DO45 K=1,10
A=0.95
NN=NN+1
DO40 I=1,21
A=A+0.05
C=1.0/0.95
DO30 N=1,21
C=C/(1.0+0.05*C)
SET LIMITS FOR NUMERICAL INTEGRATION (THESE LIMITS
BELOW HAVE BEEN PREVIOUSLY TESTED FOR CONVERGENCE)
AA=0.0
BB=1000000
IF(NN.EQ.10) BB=500000000
MAXDIV=50
EPS=1.0E-08
ACC=0.0
IFAIL=0
CALL U.K. "NAG" LIBRARY ROUTINE FOR NUMERICAL EVALUATION
OF THE INTEGRALS "ALPHA" GIVEN IN THE SUBROUTINE BELOW
CALL DD1AGF(AA,BB,FUN,MAXDIV,EPS,ACC,ANS,ERROR,NOFUN,IFAIL)
ALPHA(NN,I,N)=ANS
30 CONTINUE
40 CONTINUE
45 CONTINUE
B=1.0
A=0.95
DO80 J=1,21
A=A+0.05
C=1.0/0.95
DO70 N=1,21
C=C/(1.0+0.05*C)
NOW COMPUTE THE FUNCTION VALUES USING THE STORED INTEGRAL VALUES
NU(J,N)=(1.0/(A*B*C))*((4.0/15.0)*((ALPHA(7,J,N)+ALPHA(8,J,N)
+ ALPHA(9,J,N))/(ALPHA(8,J,N)*ALPHA(9,J,N)+ALPHA(9,J,N)*ALPHA
+ (7,J,N)+ALPHA(7,J,N)*ALPHA(8,J,N)))+(1.0/5.0)*(((ALPHA(2,J,N)
+ ALPHA(3,J,N))/(ALPHA(4,J,N)*(B*B*ALPHA(2,J,N)+C*C*ALPHA(3,J,N)
+ )))+(ALPHA(3,J,N)+ALPHA(1,J,N))/(ALPHA(5,J,N)*(C*C*ALPHA(3,J,N)
+ A*A*ALPHA(1,J,N)))+(ALPHA(1,J,N)+ALPHA(2,J,N))/(ALPHA(6,J,N)
+ (A*A*ALPHA(1,J,N)+B*B*ALPHA(2,J,N))))))
F(J,N)=2.0/(((A*B*C)**(1.0/3.0))*ALPHA(10,J,N))
R(J,N)=2.0*(1.0+(F(J,N)**3.0))/NU(J,N)
BETA(J,N)=(1.0/1000000.0)*(((6.0249**((1.0/3.0))*((10.0**((23.0/3.0)
+ )))/(16200.0*3.141592654*3.141592654)**(1.0/3.0)))*(NU(J,N)
+ ((1.0/3.0))/F(J,N))
M(J,N)=(B*B+C*C)/(B*B*ALPHA(2,J,N)+C*C*ALPHA(3,J,N))
O(J,N)=(C*C+A*A)/(C*C*ALPHA(3,J,N)+A*A*ALPHA(1,J,N))
P(J,N)=(A*A+B*B)/(A*A*ALPHA(1,J,N)+B*B*ALPHA(2,J,N))
TPLS(J,N)=((A*B*C)/(12.0))*(((1.0/M(J,N)))+(1.0/O(J,N)))+(1.0/P(J,
+ N)))+(1.0/M(J,N)**2.0)+(1.0/O(J,N)**2.0)+(1.0/P(J,N)**2.0))-
+ ((1.0/(M(J,N)*O(J,N)))+(1.0/(O(J,N)*P(J,N)))+(1.0/(P(J,N)*M(J,
+ N))))**0.5))
TMNS(J,N)=((A*B*C)/(12.0))*(((1.0/M(J,N)))+(1.0/O(J,N)))+(1.0/P(J,
+ N)))-(((1.0/M(J,N)**2.0)+(1.0/O(J,N)**2.0)+(1.0/P(J,N)**2.0))-
+ ((1.0/(M(J,N)*O(J,N)))+(1.0/(O(J,N)*P(J,N)))+(1.0/(P(J,N)*M(J,
+ N))))**0.5))
CA(J,N)=(2.0/(3.0*A*B*C))*M(J,N)
CB(J,N)=(2.0/(3.0*A*B*C))*O(J,N)

```

```

CC(J,N)=(2.0/(3.0*A*B*C))*P(J,N)
RHOA(J,N)=2.0/((1.0/CB(J,N))+(1.0/CC(J,N)))
RHOB(J,N)=2.0/((1.0/CA(J,N))+(1.0/CC(J,N)))
RHOC(J,N)=2.0/((1.0/CA(J,N))+(1.0/CB(J,N)))
DELA(J,N)=NU(J,N)/CA(J,N)
DELB(J,N)=NU(J,N)/CB(J,N)
DELC(J,N)=NU(J,N)/CC(J,N)
TAU(J,N)=3.0/((1.0/CA(J,N))+(1.0/CB(J,N))+(1.0/CC(J,N)))
PSI(J,N)=F(J,N)*((1.0/TAU(J,N))**2.0)
V(J,N)=NU(J,N)/TAU(J,N)
X1(J,N)=0.5*((1.0/RHOB(J,N))+(1.0/RHOC(J,N))-(1.0/RHOA(J,N)))
X2(J,N)=0.5*((1.0/RHOC(J,N))+(1.0/RHOA(J,N))-(1.0/RHOB(J,N)))
X3(J,N)=0.5*((1.0/RHOA(J,N))+(1.0/RHOB(J,N))-(1.0/RHOC(J,N)))
X4(J,N)=(X1(J,N)+X2(J,N)+X3(J,N))/3.0
X5(J,N)=((X1(J,N)**2.0)+(X2(J,N)**2.0)+(X3(J,N)**2.0)-(X1(J,N)*X2
+ (J,N))-(X2(J,N)*X3(J,N))-(X3(J,N)*X1(J,N)))**0.5
T1(J,N)=1.0/(X4(J,N)+X1(J,N))
T2(J,N)=1.0/(X4(J,N)+X2(J,N))
T3(J,N)=1.0/(X4(J,N)+X3(J,N))
T4(J,N)=3.0/((6.0*X4(J,N))-(2.0*X5(J,N)))
T5(J,N)=3.0/((6.0*X4(J,N))+(2.0*X5(J,N)))
GAMMAA(J,N)=(1.0/2.0)*(F(J,N)**3.0)*((1.0/CB(J,N))+(1.0/CC(J,N)))
GAMMAB(J,N)=(1.0/2.0)*(F(J,N)**3.0)*((1.0/CA(J,N))+(1.0/CC(J,N)))
GAMMAC(J,N)=(1.0/2.0)*(F(J,N)**3.0)*((1.0/CA(J,N))+(1.0/CB(J,N)))
MUA(J,N)=(CA(J,N)**(1.0/3.0))/F(J,N)
MUB(J,N)=(CB(J,N)**(1.0/3.0))/F(J,N)
MUC(J,N)=(CC(J,N)**(1.0/3.0))/F(J,N)
DPLS(J,N)=6.0*TPLS(J,N)*NU(J,N)
DMNS(J,N)=6.0*TMNS(J,N)*NU(J,N)
GPLS(J,N)=6.0*TPLS(J,N)*(F(J,N)**3.0)
GMNS(J,N)=6.0*TMNS(J,N)*(F(J,N)**3.0)
70 CONTINUE
80 CONTINUE
CALL PAPER(1)
CALL MAP(1.0,2.0,1.0,2.0)
CALL SCALSI(0.1,0.1)
CALL GPSTOP(21)
CALL BORDER
CALL CSPACE(0.0,0.0001,0.0,0.0001)

(I) PLOT OF VISCOSITY INCREMENT AND PERRIN TRANSLATIONAL
    FRICTIONAL FUNCTION

H(1)=2.892
CALL CONTRL(NU,1,21,21,1,21,21,H,1,1)
CALL REDPEN
H(1)=1.044
CALL CONTRL(F,1,21,21,1,21,21,H,1,1)

(II) PLOT OF THE TRANSLATIONAL FUNCTIONS: THE VISCOSITY INCREMENT
    THE PERRIN FUNCTION, THE BETA FUNCTION AND THE R FUNCTION, ALL
    WITH +/-1% ASSUMED EXPERIMENTAL ERROR

CALL FRAME
CALL BLKPEN
CALL BORDER
CALL CSPACE(0.0,1.0,0.0,1.0)
CALL SCALSI(0.1,0.1)
CALL CSPACE(0.0,0.0001,0.0,0.0001)
H(1)=2.92092
CALL CONTRL(NU,1,21,21,1,21,21,H,1,1)
H(1)=2.86308
CALL CONTRL(NU,1,21,21,1,21,21,H,1,1)
H(1)=2.14423
CALL REDPEN
CALL CONTRL(BETA,1,21,21,1,21,21,H,1,1)
H(1)=2.10177
CALL CONTRL(BETA,1,21,21,1,21,21,H,1,1)
H(1)=1.05444
CALL GRNPEN
CALL CONTRL(F,1,21,21,1,21,21,H,1,1)
H(1)=1.03356
CALL CONTRL(F,1,21,21,1,21,21,H,1,1)
H(1)=1.49379
CALL BROKEN(4,8,8,8)
CALL CONTRL(R,1,21,21,1,21,21,H,1,1)
H(1)=1.46421
CALL CONTRL(R,1,21,21,1,21,21,H,1,1)

(III) PLOT OF THE R FUNCTION AND ROTATIONAL RELAXATION
    TIME RATIOS

```

C

```
CALL FRAME
CALL FULL
CALL BLKPEN
CALL BORDER
CALL CSPACE(0.0,1.0,0.0,1.0)
CALL SCALSI(0.1,0.1)
CALL CSPACE(0.0,0.0001,0.0,0.0001)
H(1)=1.479
CALL CONTRL(R,1,21,21,1,21,21,H,1,1)
H(1)=1.433
CALL CONTRL(RHOA,1,21,21,1,21,21,H,1,1)
H(1)=1.115
CALL REDPEN
CALL CONTRL(RHOB,1,21,21,1,21,21,H,1,1)
H(1)=1.093
CALL GRNPEN
CALL CONTRL(RHOC,1,21,21,1,21,21,H,1,1)
```

```

CALL CONTRL(R,1,21,21,1,21,21,H,1,1)
H(1)=1.46421
CALL CONTRL(R,1,21,21,1,21,21,H,1,1)
H(1)=3.2849
CALL CONTRL(DELA,1,21,21,1,21,21,H,1,1)
H(1)=3.1560802
CALL CONTRL(DELA,1,21,21,1,21,21,H,1,1)
H(1)=2.110
CALL REDPEN
CALL CONTRL(DELB,1,21,21,1,21,21,H,1,1)
H(1)=2.072
CALL CONTRL(DELB,1,21,21,1,21,21,H,1,1)
H(1)=2.006
CALL GRNPEN
CALL CONTRL(DELC,1,21,21,1,21,21,H,1,1)
H(1)=1.928
CALL CONTRL(DELC,1,21,21,1,21,21,H,1,1)

```

(VII) PLOT OF THE R, GAMMAA, GAMMAB AND GAMMAC FUNCTIONS

```

CALL FRAME
CALL BLKPEN
CALL BORDER
CALL CSPACE(0.0,1.0,0.0,1.0)
CALL SCALSI(0.1,0.1)
CALL CSPACE(0.0,0.0001,0.0,0.0001)
H(1)=1.479
CALL CONTRL(R,1,21,21,1,21,21,H,1,1)
H(1)=0.795
CALL CONTRL(GAMMAA,1,21,21,1,21,21,H,1,1)
H(1)=1.022
CALL REDPEN
CALL CONTRL(GAMMAB,1,21,21,1,21,21,H,1,1)
H(1)=1.042
CALL GRNPEN
CALL CONTRL(GAMMAC,1,21,21,1,21,21,H,1,1)

```

(VIII) PLOT OF R (+/-1%), GAMMAA (+/-1%), GAMMAB (+/-1%) AND GAMMAC (+/-1%)

```

CALL FRAME
CALL BLKPEN
CALL BORDER
CALL CSPACE(0.0,1.0,0.0,1.0)
CALL SCALSI(0.1,0.1)
CALL CSPACE(0.0,0.0001,0.0,0.0001)
H(1)=1.49379
CALL CONTRL(R,1,21,21,1,21,21,H,1,1)
H(1)=1.46421
CALL CONTRL(R,1,21,21,1,21,21,H,1,1)
H(1)=.81498
CALL CONTRL(GAMMAA,1,21,21,1,21,21,H,1,1)
H(1)=.78302
CALL CONTRL(GAMMAA,1,21,21,1,21,21,H,1,1)
H(1)=1.04244
CALL REDPEN
CALL CONTRL(GAMMAB,1,21,21,1,21,21,H,1,1)
H(1)=1.00156
CALL CONTRL(GAMMAB,1,21,21,1,21,21,H,1,1)
CALL GRNPEN
H(1)=1.06284
CALL CONTRL(GAMMAC,1,21,21,1,21,21,H,1,1)
H(1)=1.02116
CALL CONTRL(GAMMAC,1,21,21,1,21,21,H,1,1)

```

(IX) PLOT OF THE R, MUA, MUB AND MUC FUNCTIONS

```

CALL FRAME
CALL BLKPEN
CALL BORDER
CALL CSPACE(0.0,1.0,0.0,1.0)
CALL SCALSI(0.1,0.1)
CALL CSPACE(0.0,0.0001,0.0,0.0001)
H(1)=1.479
CALL CONTRL(R,1,21,21,1,21,21,H,1,1)
H(1)=.924
CALL CONTRL(MUA,1,21,21,1,21,21,H,1,1)
CALL REDPEN
H(1)=1.071
CALL CONTRL(MUB,1,21,21,1,21,21,H,1,1)

```

```

CALL GRNPEN
H(1)=1.089
CALL CONTRL(MUC,1,21,21,1,21,21,H,1,1)

```

```

(X)PLOT OF R (+/-1%), MUA (+/-1%), MUB (+/-1%)
AND MUC (+/-1%)

```

```

CALL FRAME
CALL BLKPEN
CALL BORDER
CALL CSPACE(0.0,1.0,0.0,1.0)
CALL SCALSI(0.1,0.1)
CALL CSPACE(0.0,0.0001,0.0,0.0001)
H(1)=1.49379
CALL CONTRL(R,1,21,21,1,21,21,H,1,1)
H(1)=1.46421
CALL CONTRL(R,1,21,21,1,21,21,H,1,1)
H(1)=.94248
CALL CONTRL(MUA,1,21,21,1,21,21,H,1,1)
H(1)=.90552
CALL CONTRL(MUA,1,21,21,1,21,21,H,1,1)
H(1)=1.90242
CALL REDPEN
CALL CONTRL(MUB,1,21,21,1,21,21,H,1,1)
H(1)=1.04958
CALL CONTRL(MUB,1,21,21,1,21,21,H,1,1)
H(1)=1.11078
CALL GRNPEN
CALL CONTRL(MUC,1,21,21,1,21,21,H,1,1)
H(1)=1.06722
CALL CONTRL(MUC,1,21,21,1,21,21,H,1,1)

```

```

(XI)PLOT OF THE R, REDUCED THETA+ AND REDUCED
THETA - FUNCTIONS

```

```

CALL FRAME
CALL BLKPEN
CALL BORDER
CALL CSPACE(0.0,1.0,0.0,1.0)
CALL SCALSI(0.1,0.1)
CALL CSPACE(0.0,0.0001,0.0,0.0001)
H(1)=1.479
CALL CONTRL(R,1,21,21,1,21,21,H,1,1)
CALL REDPEN
H(1)=.163
CALL CONTRL(TPLS,1,21,21,1,21,21,H,1,1)
CALL GRNPEN
H(1)=.116
CALL CONTRL(TMNS,1,21,21,1,21,21,H,1,1)

```

```

(XII)PLOT OF THE R(+/-1%), REDUCED THETA+ (+/-1%)
AND REDUCED THETA- (+/-1%) FUNCTIONS

```

```

CALL FRAME
CALL BLKPEN
CALL BORDER
CALL CSPACE(0.0,1.0,0.0,1.0)
CALL SCALSI(0.1,0.1)
CALL CSPACE(0.0,0.0001,0.0,0.0001)
H(1)=1.49379
CALL CONTRL(R,1,21,21,1,21,21,H,1,1)
H(1)=1.46421
CALL CONTRL(R,1,21,21,1,21,21,H,1,1)
CALL REDPEN
H(1)=.16463
CALL CONTRL(TPLS,1,21,21,1,21,21,H,1,1)
H(1)=.16137
CALL CONTRL(TPLS,1,21,21,1,21,21,H,1,1)
CALL GRNPEN
H(1)=.11716
CALL CONTRL(TMNS,1,21,21,1,21,21,H,1,1)
H(1)=.11484
CALL CONTRL(TMNS,1,21,21,1,21,21,H,1,1)

```

```

(XIII)PLOT OF THE R, DELTA+ AND DELTA- FUNCTIONS

```

```

CALL FRAME
CALL BLKPEN
CALL BORDER
CALL CSPACE(0.0,1.0,0.0,1.0)
CALL SCALSI(0.1,0.1)
CALL CSPACE(0.0,0.0001,0.0,0.0001)
H(1)=1.479
CALL CONTRL(R,1,21,21,1,21,21,H,1,1)
CALL REDPEN
H(1)=2.821
CALL CONTRL(DPLS,1,21,21,1,21,21,H,1,1)
CALL GRNPEN
H(1)=2.016
CALL CONTRL(DMNS,1,21,21,1,21,21,H,1,1)

```

(XIV) PLOT OF R ($\pm 1\%$), DELTA+ ($\pm 2\%$) AND DELTA- ($\pm 2\%$)

```

CALL FRAME
CALL BLKPEN
CALL BORDER
CALL CSPACE(0.0,1.0,0.0,1.0)
CALL SCALSI(0.1,0.1)
CALL CSPACE(0.0,0.0001,0.0,0.0001)
H(1)=1.49379
CALL CONTRL(R,1,21,21,1,21,21,H,1,1)
H(1)=1.46421
CALL CONTRL(R,1,21,21,1,21,21,H,1,1)
CALL REDPEN
H(1)=2.87742
CALL CONTRL(DPLS,1,21,21,1,21,21,H,1,1)
H(1)=2.76458
CALL CONTRL(DPLS,1,21,21,1,21,21,H,1,1)
CALL GRNPEN
H(1)=2.05632
CALL CONTRL(DMNS,1,21,21,1,21,21,H,1,1)
H(1)=1.97568
CALL CONTRL(DMNS,1,21,21,1,21,21,H,1,1)

```

(XV) PLOT OF THE R, GAMMA+ AND GAMMA- FUNCTIONS

```

CALL FRAME
CALL BLKPEN
CALL BORDER
CALL CSPACE(0.0,1.0,0.0,1.0)
CALL SCALSI(0.1,0.1)
CALL CSPACE(0.0,0.0001,0.0,0.0001)
H(1)=1.479
CALL CONTRL(R,1,21,21,1,21,21,H,1,1)
CALL REDPEN
H(1)=1.111
CALL CONTRL(GPLS,1,21,21,1,21,21,H,1,1)
CALL GRNPEN
CALL CONTRL(GMNS,1,21,21,1,21,21,H,1,1)

```

(XVI) PLOT OF R ($\pm 1\%$), GAMMA+ ($\pm 2\%$) AND GAMMA- ($\pm 2\%$)

```

CALL FRAME
CALL BLKPEN
CALL BORDER
CALL CSPACE(0.0,1.0,0.0,1.0)
CALL SCALSI(0.1,0.1)
CALL CSPACE(0.0,0.0001,0.0,0.0001)
H(1)=1.49379
CALL CONTRL(R,1,21,21,1,21,21,H,1,1)
H(1)=1.46421
CALL CONTRL(R,1,21,21,1,21,21,H,1,1)
CALL REDPEN
H(1)=1.13322
CALL CONTRL(GPLS,1,21,21,1,21,21,H,1,1)
H(1)=1.08878
CALL CONTRL(GPLS,1,21,21,1,21,21,H,1,1)
CALL GRNPEN
H(1)=.80988
CALL CONTRL(GMNS,1,21,21,1,21,21,H,1,1)
H(1)=.77812

```

```
CALL CONTRL(GMNS,1,21,21,1,21,21,H,1,1)
```

```
(XVII) PLOT OF THE 5 FLUORESCENCE ANISOTROPY RELAXATION TIME RATIOS
```

```
CALL FRAME
CALL BLKPEN
CALL BORDER
CALL CSPACE(0.0,1.0,0.0,1.0)
CALL SCALSI(0.1,0.1)
CALL CSPACE(0.0,0.0001,0.0,0.0001)
H(1)=1.02536
CALL CONTRL(T1,1,21,21,1,21,21,H,1,1)
H(1)=1.28883
CALL REDPEN
CALL CONTRL(T2,1,21,21,1,21,21,H,1,1)
CALL GRNPEN
H(1)=1.31877
CALL CONTRL(T3,1,21,21,1,21,21,H,1,1)
CALL BROKEN(4,8,8,8)
H(1)=1.43405
CALL CONTRL(T4,1,21,21,1,21,21,H,1,1)
CALL BLKPEN
H(1)=1.02497
CALL CONTRL(T5,1,21,21,1,21,21,H,1,1)
STOP
END
```

```
REAL FUNCTION FUN(X)
```

```
COMMON/PARAM/A,C,NN
```

```
B=1.0
```

```
GOTO(10,20,30,40,50,60,70,80,90,100),NN
```

```
10 FUN=1/((A*A+X)**1.5*(B*B+X)**0.5*(C*C+X)**0.5)
```

```
RETURN
```

```
20 FUN=1/((A*A+X)**0.5*(B*B+X)**1.5*(C*C+X)**0.5)
```

```
RETURN
```

```
30 FUN=1/((A*A+X)**0.5*(B*B+X)**0.5*(C*C+X)**1.5)
```

```
RETURN
```

```
40 FUN=1/((A*A+X)**0.5*(B*B+X)**1.5*(C*C+X)**1.5)
```

```
RETURN
```

```
50 FUN=1/((A*A+X)**1.5*(B*B+X)**0.5*(C*C+X)**1.5)
```

```
RETURN
```

```
60 FUN=1/((A*A+X)**1.5*(B*B+X)**1.5*(C*C+X)**0.5)
```

```
RETURN
```

```
70 FUN=X/((A*A+X)**0.5*(B*B+X)**1.5*(C*C+X)**1.5)
```

```
RETURN
```

```
80 FUN=X/((A*A+X)**1.5*(B*B+X)**0.5*(C*C+X)**1.5)
```

```
RETURN
```

```
90 FUN=X/((A*A+X)**1.5*(B*B+X)**1.5*(C*C+X)**0.5)
```

```
RETURN
```

```
100 FUN=1.0/((A*A+X)*(B*B+X)*(C*C+X))**0.5)
```

```
RETURN
```

```
END
```

Program 5

```

C NON-LINEAR LEAST SQUARES METHOD USING AN ALGORITHM OF GILL AND
C MURRAY (1976)
C
C GAMMA = BIREFRINGENCE (RADS), F = SUM OF SQUARES OF THE RESIDUALS
C DPLS = DELTA+, DMNS = DELTA-
C X(1) = CURRENT INITIAL GUESS FOR THETA+
C X(2) = " " " " " " " " " "
C X(3) = " " " " " " " " " "
C X(4) = " " " " " " " " " "
C X1 = CURRENT ESTIMATE FOR THETA+
C X2 = " " " " " " " " " "
C X3 = " " " " " " " " " "
C X4 = " " " " " " " " " "
C
C *****
C LINEAR TIME INCREASE, 100PTS.
C .001 DEGREES S.E.
C
C RANDOM NUMBER RUN 50
C
C *****
C PROTEIN 3
C
C *****
C PROGRAM MAIN(INPUT,OUTPUT,TAPE2=INPUT,TAPE3=OUTPUT)
C COMMON/PARAM/GAMMA(101),T(101),R(101)
C REAL BL(4),BU(4),X(4),F,W(54)
C REAL Q1,Q2,Q3,Q4,Q5
C INTEGER IBOUND,IFAIL,J,LIW,LW,N
C INTEGER IW(6)
C P=-1.0
C DO21 I=1,101
C P=P+1.0
C R(I)=P
C T(I)=R(I)*1.0E-09
C 21 CONTINUE
C WRITE(3,32)
C 32 FORMAT(" TIME(NS) GAMMA")
C G05BBF REINITIALIZES THE STREAM OF THE RANDOM NUMBERS
C CALL G05BBF
C CALCULATE THE UNPERTURBED DECAY CURVE
C DO50 I=1,101
C GAMMA(I)=0.07*EXP(-T(I)*6.0*5.187243E06)+
C +0.05*EXP(-T(I)*6.0*4.167486E06)
C NOW PERTURB EACH OF THE 160 DATA POINTS USING A NORMAL PSEUDO-RANDOM
C NUMBER GENERATOR G05ADF
C GAMMA(I)=GAMMA(I)+((0.1*1.74555E-04)*G05ADF(Y))
C WRITE(3,33)R(I),GAMMA(I)
C 33 FORMAT(F10.5,F8.5)
C 50 CONTINUE
C N=4
C IBOUND=0
C Q1=1.0
C DO THE MINIMIZATION FOR 30 INITIAL GUESSES TO ATTEMPT TO AVOID
C SUBSIDIARY MINIMA
C DO10 I=1,30
C CALL RECTANGULAR PSEUDO RANDOM NUMBER ROUTINE G05AAF
C Z=G05AAF(X)
C X(1)=4.0+2.0*Z
C X(2)=3.0+2.0*Z
C X(3)=6.0+2.0*Z
C X(4)=4.0+2.0*Z
C BL(1)=4.0
C BL(2)=3.0
C BL(3)=6.0
C BL(4)=4.0
C BU(1)=6.0
C BU(2)=5.0
C BU(3)=8.0
C BU(4)=6.0
C LIW=6
C LW=54
C IFAIL=1
C CALL E04JAF(N,IBOUND,BL,BU,X,F,IW,LIW,W,LW,IFAIL)
C IF(IFAIL.NE.0)WRITE(3,100)IFAIL
C IF(IFAIL.EQ.1)GOTO 20
C 100 FORMAT("ERROR EXIT TYPE",I3,"SEE ROUTINE MANUAL")
C WRITE(3,110)F
C WRITE(3,120)(X(J),J=1,4)
C 110 FORMAT(" FUNCTION VALUE ON EXIT IS",F15.12)

```

```

120 FORMAT( " THETA+",F10.7," THETA-",F10.7,"A ",F7.4,
+ " A-",F7.4)
IF(Q1.LE.F)GOTO 30
Q1=F
Q2=X(1)
Q3=X(2)
Q4=X(3)
Q5=X(4)
30 CONTINUE
WRITE(3,130)
130 FORMAT( " ")
WRITE(3,140)
140 FORMAT( " ")
10 CONTINUE
DPLS=0.50996303*Q2
DMNS=0.50996303*Q3
WRITE(3,141)
141 FORMAT( " ")
WRITE(3,142)
142 FORMAT( " ")
WRITE(3,143)
143 FORMAT( " ")
WRITE(3,145)
145 FORMAT( " ")
WRITE(3,150)Q1
150 FORMAT( " BEST LEAST SQUARES VALUE = ",F15.12)
WRITE(3,160)Q2
160 FORMAT( " THETA+ = ",F10.7)
WRITE(3,170)Q3
170 FORMAT( " THETA- = ",F10.7)
WRITE(3,180)Q4
180 FORMAT( " A'+ = ",F7.4)
WRITE(3,190)Q5
190 FORMAT( " A'- = ",F7.4)
WRITE(3,200)DPLS
200 FORMAT( " DELTA+ = ",F10.7)
WRITE(3,210)DMNS
210 FORMAT( " DELTA- = ",F10.7)
20 STOP
END

```

C SUBROUTINE FOR CALCULATING THE SUM OF SQUARES OF THE RESIDUALS FOR THE
C CURRENT ESTIMATES OF THE ADJUSTABLE PARAMETERS

```

SUBROUTINE FUNCT1(N,XC,FC)
COMMON/PARAM/GAMMA(101),T(101),R(101)
EXTERNAL FUN
REAL Q,FC
INTEGER N
REAL XC(N)
REAL X1,X2,X3,X4
X1=XC(1)
X2=XC(2)
X3=XC(3)
X4=XC(4)
FC=0.0
DO75 I=1,101
Q=(GAMMA(I)-(0.01*X3*EXP(-6.0E06*X1*T(I))+0.01*X4
+ *EXP(-6.0E06*X2*T(I))))**2.0
FC=FC+Q
75 CONTINUE
RETURN
END

```

Program 6

FOURIER TRANSFORM SOLUTION OF THE LAPLACE INTEGRAL EQUATION METHOD OF
GARDNER, GARDNER, LAUSH AND MEINKE (1959)

S = BIREFRINGENCE (RADS), GM = INTEGRAND OF EQUATION, G = G(EXP(-Y))
T = TIME (SEC), R = TIME (NS), EC AND ES ARE THE ERROR ESTIMATES IN FC
AND FS RESPECTIVELY DUE TO THE NUMERICAL INTEGRATION IN EQN. 125
AND ER IS THE ERROR ESTIMATE DUE TO THE NUMERICAL INTEGRATION IN
EQN. 128

LOGARITHMIC TIME INCREASE, 140 DATA PTS.
.001 DEGREES S.E.

RANDOM NUMBER RUN 2

PROTEIN 2

PROGRAM MAIN(INPUT,OUTPUT,TAPE2=INPUT,TAPE3=OUTPUT)
EXTERNAL FUNXN
REAL MMU(66),KC(66),KS(66),FC(66),FS(66),GM(66),MU
REAL YYY,G(690),Y(690),EC(66),ES(66)
INTEGER N,I,IFAIL
INTEGER L
REAL X(141),S(141),R(141),T(141),YC(141),YS(141)
COMPLEX Z,C,K,CGAMMA
P=-7.1

DO21 I=1,141

P=P+.1

WRITE(3,500)

500 FORMAT(" ")

X(I)=P

T(I)=(1.0E-09)*EXP(X(I))

R(I)=T(I)*1.0E09

21 CONTINUE

WRITE(3,32)

32 FORMAT(" " TIME(NS) X S(T) = S(EXP(-X)) ")

WRITE(3,501)

501 FORMAT(" ")

WRITE(3,502)

502 FORMAT(" ***** ")

WRITE(3,503)

503 FORMAT(" ")

C G05BBF REINITIALIZES THE STREAM OF THE RANDOM NUMBERS

CALL G05BBF

DO50 I=1,141

C CALCULATE THE UNPERTURBED DECAY CURVE

S(I)=0.07*EXP(-T(I)*4.6596278E07)+

+0.05*EXP(-T(I)*3.137407E07)

C NOW PERTURB EACH OF THE 140 DATA PTS USING A NORMAL PSEUDO-RANDOM

C NUMBER GENERATOR

S(I)=S(I)+((0.1*1.74555E-04)*G05ADF(Y))

WRITE(3,33)R(I),X(I),S(I)

33 FORMAT(F10.5,F6.2,F8.5)

50 CONTINUE

DO47 L=1,20

WRITE(3,504)

504 FORMAT(" ")

47 CONTINUE

C THE NEXT PART OF THE PROGRAM EVALUATES THE FOURIER TRANSFORM OF THE DATA

MU=-.1

WRITE(3,99)

99 FORMAT(" " MU KC KS ")

WRITE(3,505)

505 FORMAT(" ")

WRITE(3,506)

506 FORMAT(" ***** ")

WRITE(3,507)

507 FORMAT(" ")

DO10 J=1,66

MU=MU+.1

MMU(J)=MU

DO51 I=1,141

YC(I)=(EXP(X(I)))*S(I)*COS(MU*X(I))

YS(I)=(EXP(X(I)))*S(I)*SIN(MU*X(I))

Y(I)=CMPLX(YC(I),YS(I))

51 CONTINUE

N=141

IFAIL=1

```

C CALL NUMERICAL INTEGRATION ROUTINE FROM THE UK NAG LIBRARY (MK 6)
  CALL D01GAF(X,YC,N,ANS,ER,IFAIL)
  FC(J)=((1.0/(2.0*3.141593))**0.5)*ANS
  EC(J)=((1.0/(2.0*3.141593))**0.5)*ER
  CALL D01GAF(X,YS,N,ANS,ER,IFAIL)
  FS(J)=((1.0/(2.0*3.141593))**0.5)*ANS
  ES(J)=((1.0/(2.0*3.141593))**0.5)*ER
C EVALUATE THE COMPLEX GAMMA FUNCTION FOR THE CURRENT VALUE OF MU USING
C THE SUBROUTINE BELOW
  Z=CMPLX(1.0,MU)
  C=CGAMMA(Z)
C DETERMINE THE EULER INTEGRAL OF THE COMPLEX GAMMA FUNCTION (EQN. 123 )
  K=((1.0/(2.0*3.141593))**0.5)*C
  KC(J)=REAL(K)
  KS(J)=AIMAG(K)
  C=CGAMMA(Z)
  WRITE(3,101)MU,K
101  FORMAT(7X,1F8.2,2E15.7)
  10  CONTINUE
  DO49 L=1,20
  WRITE(3,509)
509  FORMAT(" ")
  49  CONTINUE
  WRITE(3,90)
  90  FORMAT("      MU          FC          (ERR)          FS
+      (ERR)")
  WRITE(3,510)
510  FORMAT(" ")
  WRITE(3,511)
511  FORMAT("*****")
  WRITE(3,512)
512  FORMAT(" ")
  DO38 J=1,66
  WRITE(3,91)MMU(J),FC(J),EC(J),FS(J),ES(J)
  91  FORMAT(1X,1F8.2,4E14.7)
  38  CONTINUE
  DO52 L=1,20
  WRITE(3,513)
513  FORMAT(" ")
  52  CONTINUE
  WRITE(3,93)
  93  FORMAT("      Y          G(EXP(-Y))          ERROR")
  WRITE(3,514)
514  FORMAT(" ")
  WRITE(3,515)
515  FORMAT("*****")
  WRITE(3,516)
516  FORMAT(" ")
  YYY=-.01
  DO31 M=1,690
  YYY=YYY+.01
  Y(M)=YYY
  DO29 J=1,66
C DIVIDE THE FOURIER TRANSFORM OF THE DATA BY THE EULER INTEGRAL FOR THE
C COMPLEX GAMMA FUNCTION
  GM(J)=((((FC(J)*KC(J)))+(FS(J)*KS(J)))*COS(YYY*MMU(J)))/((KC(J)
+KC(J))
+((KS(J)*KS(J)))+((((FS(J)*KC(J))-(FC(J)*KS(J)))*SIN(YYY*MMU(J)))/
+((KC(J)*KC(J))+(KS(J)*KS(J))))
  29  CONTINUE
  NN=66
C NOW G(EXP(-Y)) AS A FUNCTION OF Y IS FOUND FROM THE INVERSE FOURIER
C TRANSFORM USING THE SAME NUMERICAL INTEGRATION ROUTINE
  CALL D01GAF(MMU,GM,NN,ANS,ER,IFAIL)
  G(M)=(1.0/3.141593)*ANS
  ER=(1.0/3.141593)*ER
  WRITE(3,290)YYY,G(M),ER
  IF(IFAIL)241,261,241
241  WRITE(3,289)
261  CONTINUE
290  FORMAT(/3X,F7.2,4X,1E15.7,4X,1E15.7)
289  FORMAT(/28H LESS THAN 4 POINTS SUPPLIED)
  31  CONTINUE
C HENCE A PLOT OF G(EXP(-Y)) AGAINST Y IS OBTAINED
  CALL PAPER(1)
  CALL MAP(0.0,0.0,0.0,0.0)
  CALL CURVEO(Y,G,1,690)
  CALL SCALES
  CALL BORDER
  CALL GRAPHF(FUNXN)

```

```

CALL GREND
STOP
END

```

```

C
FUNCTION FUNXN(X)
FUNXN=0.0
RETURN
END

```

```

C SUBROUTINE FOR CALCULATING THE COMPLEX GAMMA FUNCTION C = CGAMMA(Z) FOR
C THE CURRENT VALUE OF MU. THIS SUBROUTINE IS THAT GIVEN BY LUCAS AND
C TERRILL (1970)
C COMPLEX FUNCTION CGAMMA(Z)
C COMPLEX Z,ZM,T,TT,SUM,TERM,DEN,PI,A
C DIMENSION C(12)
C LOGICAL REFLEX
C SET IOUT FOR PROPER OUTPUT CHANNEL OF COMPUTER SYSTEM FOR
C ERROR MESSAGES
C IOUT=3
C PI=(3.141593,0.0)
C X=REAL(Z)
C Y=AIMAG(Z)
C TOL = LIMIT OF PRECISION OF COMPUTER SYSTEM IN SINGLE PRECISION
C TOL=1.0E-07
C REFLEX=.TRUE.
C DETERMINE WHETHER Z IS TOO CLOSE TO A POLE
C CHECK WHETHER TOO CLOSE TO ORIGIN
C IF(X.GE.TOL) GO TO 20
C FIND THE NEAREST POLE AND COMPUTE DISTANCE TO IT
C XDIST=X-INT(X-.5)
C ZM=CMPLX(XDIST,Y)
C IF(CABS(ZM).GE.TOL)GOTO 10
C IF Z IS TOO CLOSE TO A POLE, PRINT ERROR MESSAGE AND RETURN
C WITH CGAMMA=(1.E7,0.F0)
C WRITE (IOUT,900)Z
C CGAMMA=(1.E7,0.E0)
C RETURN
C FOR REAL(Z) NEGATIVE EMPLOY THE REFLECTION FORMULA
C GAMMA(Z)=PI(SINPI*Z)*GAMMA(1-Z))
C AND COMPUTE GAMMA(1-Z). NOTE REFLEX IS A TAG TO INDICATE THAT
C THIS RELATION MUST BE USED LATER.
C 10 IF(X.GE.0.0)GOTO 20
C REFLEX=.FALSE.
C Z=(1.0,0.0)-Z
C X=1.0-X
C Y=-Y
C IF Z IS NOT TOO CLOSE TO A POLE, MAKE REAL(Z)>10 AND ARG(Z)<PI/4
C 20 M=0
C 40 IF(X.GE.10.)GOTO 50
C X=X+1.0
C M=M+1
C GOTO 40
C 50 IF(ABS(Y).LT.X)GOTO 60
C X=X+1.0
C M=M+1
C GOTO 50
C 60 T=CMPLX(X,Y)
C TT=T*T
C DEN=T

```

```

C COEFFICIENTS IN STIRLING'S APPROXIMATION FOR LN(GAMMA(T))
  C(1)=1./12.
  C(2)=-1./360.
  C(3)=1./1260.
  C(4)=-1./1680.
  C(5)=1./1188.
  C(6)=-691./36060.
  C(7)=1./156.
  C(8)=-3617./122400.
  C(9)=43867./244188.
  C(10)=-174611./125400.
  C(11)=77683./5796.
  SUM=(T-(.5,0.0))*CLOG(T)-T*CMPLX(.5*ALOG(2.*3.14159),0.0)
  J=1
  70 TERM=C(J)/DEN
C TEST REAL AND IMAGINARY PARTS OF LN(GAMMA(Z)) SEPARATELY FOR
C CONVERGENCE. IF Z IS REAL SKIP IMAGINARY PART OF CHECK.
  IF(ABS(REAL(TERM)/REAL(SUM)).GE.TOL)GOTO 80
  IF(Y.EQ.0.0)GOTO 100
  IF(ABS(AIMAG(TERM)/AIMAG(SUM)).LT.TOL)GOTO 100
  80 SUM=SUM+TERM
  J=J+1
  DEN=DEN*TT
C TEST FOR CONVERGENCE
  IF(J.EQ.12)GOTO 90
  GOTO 70
C STIRLINGS SERIES DID NOT CONVERGE. PRINT ERROR MESSAGE AND
C PROCEED
  90 WRITE(IOUT,910)Z
C RECURSION RELATION USED TO OBTAIN LN(GAMMA(Z))
  LN(GAMMA(Z))=LN(GAMMA(Z+M)/(Z*(Z+1)*...*(Z+M-1)))
  LN(GAMMA(Z+M))-LN(Z)-LN(Z+1)-...-LN(Z+M-1)
C
  100 IF(M.EQ.0)GOTO 120
  DO110 I=1,M
  A=CMPLX(I*1.-1.,0.0)
  110 SUM=SUM-CLOG(Z+A)
C CHECK TO SEE IF REFLECTION FORMULA SHOULD BE USED
  120 IF(REFLEX)GOTO 130
  SUM=CLOG(PI/CSIN(PI*Z))-SUM
  Z=(1.0,0.0)-Z
  130 CGAMMA=CEXP(SUM)
  RETURN
  900 FORMAT(1X,2F14.7,10X,49HARGUMENT OF GAMMA FUNCTION IS TOO CLOSE TO
+ A POLE)
  910 FORMAT(44H ERROR - STIRLING'S SERIES HAS NOT CONVERGED/14X,4H7
+ 2E14.7)
  END

```

Program 7

```

R-CONSTRAINED NON-LINEAR LEAST SQUARES METHOD (HARDING)

GAMMA = BIREFRINGENCE (RADS), FC = SUM OF SQUARES OF THE RESIDUALS
X(1) = CURRENT INITIAL GUESS FOR A/B
X(2) = " " " " " " A+
X(3) = " " " " " " A-
ON EXIT, X(1), X(2), X(3) CONTAIN THE BEST ESTIMATES FOR THESE PARAMETERS
XC(1) = A = CURRENT ESTIMATE FOR A/B
D = 1/C = VALUE OF B/C CORRESPONDING TO THIS ESTIMATE
S = " " " " VISCOSITY INCREMENT
V = " " " " DELTA+
W = " " " " DELTA-
THPLUS = " " " " THETA+
THMINUS = " " " " THETA-
XC(2) = CURRENT ESTIMATE FOR A+
XC(3) = " " " " A-
AA1,AA2,...,AA6 ARE THE A/B COORDINATES FOR 6 PTS ON THE R-CURVE
AD1,AD2,...,AD6 " " " " B/C
THE VALUE FOR B/C CORRESPONDING TO THE CURRENT ESTIMATE FOR A/B CAN THEN
BE FOUND USING A CUBIC POLYNOMIAL INTERPOLATION PROCEDURE BETWEEN THE
SIX GIVEN POINTS. THIS IS DONE USING A LIBRARY ROUTINE E01LF1

*****
PROTEIN 1
*****
LINEAR TIME INCREASE, 100PTS.
CUT OFF TIME: 100NS
STREAM OF RANDOM NUMBERS: 3
0.1 DEG STANDARD ERROR ON EACH DATA PT.

PROGRAM MAIN(INPUT,OUTPUT,TAPE2=INPUT,TAPE3=OUTPUT)
COMMON/PARAM/GAMMA(101),T(101),A,C,D,NN,AA(6),AD(6)
REAL R(101)
REAL AA1,AA2,AA3,AA4,AA5,AA6,AD1,AD2,AD3,AD4,AD5,AD6
REAL BL(3),BU(3),X(3),F,W(39)
INTEGER IBOUND,IFAIL,J,LIW,LW,N
INTEGER IW(5)
REAL Q1,Q2,Q3,Q4
WRITE(3,37)
37 FORMAT(" PROTEIN 1, 0.1 DEG. STANDARD ERROR")
WRITE(3,38)
38 FORMAT("
+ 100NS, 100PTS")
WRITE(3,39)
39 FORMAT("
+STREAM 3")
P=-1.1
DO21 I=1,101
P=P+1.1
R(I)=P
T(I)=R(I)*1.0E-09
R(I)=T(I)*1.0E09
21 CONTINUE
G05BAF(0.3) SPECIFIES THE XTH STREAM OF THE RANDOM NUMBERS
CALL G05BAF(0.3)
DO50 I=1,101
CALCULATE THE UNPERTURBED DECAY CURVE
GAMMA(I)=0.07*EXP(-T(I)*6.0*5.815383E06)+
+0.05*EXP(-T(I)*6.0*4.1564612E06)
NOW PERTURB EACH OF THE 100 DATA POINTS USING A NORMAL PSEUDO RANDOM
NUMBER GENERATOR G05ADF
GAMMA(I)=GAMMA(I)+((1.74555E-03)*G05ADF(Y))
50 CONTINUE
READ IN THE VALUES FOR THE LOWER LIMITS FOR THE INITIAL GUESSES OF THE
A/B, A+, A- (X100), THE LOWER AND UPPER LIMITS FOR THE COMPUTER ESTIMATES
THE COORDINATES OF THE A/B VALUES AND THEN THE COORDINATES OF THE B/C
FOR THE R-CURVE TO WHICH THESE ESTIMATES ARE CONSTRAINED
READ(2,*)XX1,XX2,XX3,BBL1,BBL2,BBL3,BBU1,BBU2,BBU3,
+AA1,AA2,AA3,AA4,AA5,AA6,AD1,AD2,AD3,AD4,AD5,AD6
AA(1)=AA1
AA(2)=AA2
AA(3)=AA3
AA(4)=AA4
AA(5)=AA5
AA(6)=AA6
AD(1)=AD1
AD(2)=AD2
AD(3)=AD3
AD(4)=AD4
AD(5)=AD5

```

```

AD(6)=AD6
N=3
IBOUND=0
Q1=1.0
DO10 I=1,3
Z=G05AAF(X)
X(1)=XX1+0.2*Z
X(2)=XX2+2.0*Z
X(3)=XX3+2.0*Z
BL(1)=BBL1
BL(2)=BBL2
BL(3)=BBL3
BU(1)=BBU1
BU(2)=BBU2
BU(3)=BBU3
LIW=5
LW=39
IFAIL=1
CALL E04JAF(N,IBOUND,BL,BU,X,F,IW,LIW,W,LW,IFAIL)
IF(IFAIL.NE.0)WRITE(3,100)IFAIL
IF(IFAIL.EQ.1)GOTO 20
100 FORMAT("ERROR EXIT TYPE",I3,"SEE ROUTINE MANUAL")
X(2)=X(2)*.01
X(3)=X(3)*.01
WRITE(3,110)F
WRITE(3,120)(X(1),X(2),X(3))
110 FORMAT(" FUNCTION VALUE ON EXIT IS",F15.12)
120 FORMAT(" A/B= ",F8.5," A+=",F15.12,
+ " A-=",F15.12)
IF(Q1.LE.F)GOTO 30
Q1=F
Q2=X(1)
Q3=X(2)
Q4=X(3)
30 CONTINUE
WRITE(3,130)
130 FORMAT(" ")
WRITE(3,140)
140 FORMAT(" ")
10 CONTINUE
WRITE(3,150)Q1
150 FORMAT(" BEST LEAST SQUARES VALUE = ",F15.12)
WRITE(3,160)Q2
160 FORMAT(" A / B = ",F8.5)
WRITE(3,170)Q3
170 FORMAT(" B / C = ",F8.5)
WRITE(3,180)Q3
180 FORMAT(" A+ = ",F7.4)
WRITE(3,190)Q4
190 FORMAT(" A- = ",F7.4)
20 STOP
END

```

C
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C

SUBROUTINE FOR CALCULATING THE SUM OF THE SQUARES OF THE RESIDUALS FOR
CURRENT ESTIMATES OF A/B, A+ AND A-
KB = BOLTZMANNS CONSTANT, NA = AVOGADROS NUMBER

C CALL LIBRARY ROUTINE FOR THE CUBIC POLYNOMIAL FIT TO THE R-CURVE POINTS
C A LISTING OF THIS IS GIVEN BELOW

```

SUBROUTINE FUNCT1(N,XC,FC)
COMMON/PARAM/GAMMA(101),T(101),A,C,D,NN,AA(6),AD(6)
EXTERNAL FUN
REAL Q,FC
INTEGER N
DIMENSION ALPHA(9)
REAL XC(N)
REAL X2,X3
REAL THPLUS,THMNUS,TEMP,ETA,M,O,P,KB,NA,MW
NN=0
A=XC(1)
NM=6
IEXIT=0
CALL E01LF1(NM,AA,AD,A,D,IEXIT)
C=1.0/D
B=1.0
DO45 K=1,9
AZ=0.0
BZ=1000000
NN=NN+1
MAXDIV=50
EPS=1.0E-08
ACC=0.0
IFAIL=0
CALL D01AGF(AZ,BZ,FUN,MAXDIV,EPS,ACC,ANS,ERROR,NOFUN,IFAIL)
ALPHA(NN)=ANS
45 CONTINUE
S=(1.0/(A*B*C))*((4.0/15.0)*((ALPHA(7)+ALPHA(8)
+ ALPHA(9))/(ALPHA(8)*ALPHA(9)+ALPHA(9)*ALPHA
+ (7)+ALPHA(7)*ALPHA(8)))+(1.0/5.0)*((ALPHA(2)
+ ALPHA(3))/(ALPHA(4)*(B*B*ALPHA(2)+C*C*ALPHA(3)
+ )))+(ALPHA(3)+ALPHA(1))/(ALPHA(5)*(C*C*ALPHA(3)
+ A*A*ALPHA(1)))+(ALPHA(1)+ALPHA(2))/(ALPHA(6)
+ (A*A*ALPHA(1)+B*B*ALPHA(2))))))
M=(B*B+C*C)/(B*B*ALPHA(2)+C*C*ALPHA(3))
O=(C*C+A*A)/(C*C*ALPHA(3)+A*A*ALPHA(1))
P=(A*A+B*B)/(A*A*ALPHA(1)+B*B*ALPHA(2))
Z=((A*B*C)/(12.0))*(((1.0/M)+(1.0/O)+(1.0/P
+ ))-(((1.0/M**2.0)+(1.0/O**2.0)+(1.0/P**2.0))-
+ ((1.0/(M*O))+(1.0/(O*P))+(1.0/(P*M
+ ))))*0.5))
U=((A*B*C)/(12.0))*(((1.0/M)+(1.0/O)+(1.0/P
+ ))+(((1.0/M**2.0)+(1.0/O**2.0)+(1.0/P**2.0))-
+ ((1.0/(M*O))+(1.0/(O*P))+(1.0/(P*M
+ ))))*0.5))
V=6.0*U*S
W=6.0*Z*S
ENTER INTRINSIC VISCOSITY
ETA=2.746
ENTER TEMPERATURE
TEMP=293.0
ENTER MOLECULAR WEIGHT
MW=71744.0
KB=1.38046E-16
NA=6.0248E23
THPLUS=(NA*KB*100.0/6.0)*(TEMP/(ETA*MW))*V
THMNUS=(NA*KB*100.0/6.0)*(TEMP/(ETA*MW))*W
X2=XC(2)
X3=XC(3)
FC=0.0
DO75 I=1,101
Q=(GAMMA(I)-(0.01*X2*EXP(-6.0*THPLUS*T(I))+0.01*X3*EXP
+ (-6.0*THMNUS*T(I))))**2.0
FC=FC+Q
75 CONTINUE
RETURN
END

```

```

C LEICESTER UNIVERSITY COMPUTER LIBRARY SUBROUTINE FOR A CUBIC
C POLYNOMIAL FIT TO A SET OF POINTS (K. BRODLIE)
C
  SUBROUTINE E01LF1(N,AX,AY,X,Y,IEXIT)
    DIMENSION AX(N),AY(N)
C CHECK DATA POINTS ARE MONOTONICALLY INCREASING
    IEXIT=1
    DO 5 I=2,N
      IF (AX(I).LE.AX(I-1))RETURN
    5 CONTINUE
C CHECK THAT X IS A VALID POINT
    IEXIT=2
    IF ((AX(1)-X)*(AX(N)-X).GT.0)RETURN
C LOCATE INTERVAL IN WHICH X LIES -
    AX(J-1).LT.X.LE.AX(J)
    IEXIT=0
    Y=AY(1)
    IF (X.EQ.AX(1))RETURN
    DO 10 I=2,N
      J=I
      IF (X.LE.AX(I))GOTO 20
    10 CONTINUE
    20 CONTINUE
    Y=AY(J)
    IF (X.EQ.AX(J))RETURN
C ESTIMATE SLOPE AT AX(J-1)
    CALL E011A(N,AX,AY,J-1,G1)
C ESTIMATE SLOPE AT AX(J)
    CALL E011A(N,AX,AY,J,G2)
C CONSTRUCT INTERPOLATING CUBIC POLYNOMIAL IN INTERVAL
    D=AY(J-1)
    C=G1
    H=AX(J)-AX(J-1)
    S=(AY(J)-AY(J-1))/H
    B=(3.0*S-2.0*G1-G2)/H
    A=(G1+G2-2.0*S)/H/H
C EVALUATE POLYNOMIAL AT POINT
    H=X-AX(J-1)
    Y=((A*H+B)*H+C)*H+D
    RETURN
  END
  SUBROUTINE E011A(N,AX,AY,J,G)
    DIMENSION AX(N),AY(N)
C CALCULATE SLOPES ON EITHER SIDE OF DATA POINT
    JM1=J-1
    JP1=J+1
    IF (J.NE.1)GO TO 20
C END-POINT IS DIFFERENT
    H1=AX(2)-AX(1)
    S1=2.0*(AY(2)-AY(1))/H1-(AY(3)-AY(2))/(AX(3)-AX(2))
    GO TO 30
    20 CONTINUE
    H1=AX(J)-AX(J-1)
    S1=(AY(J)-AY(JM1))/H1
    30 CONTINUE
    IF (J.NE.N)GO TO 40
C END-POINT IS DIFFERENT
    H2=AX(N)-AX(N-1)
    S2=2.0*(AY(N)-AY(N-1))/H2-(AY(N-1)-AY(N-2))/(AX(N-1)-AX(N-2))
    GO TO 50
    40 CONTINUE
    H2=AX(JP1)-AX(J)
    S2=(AY(JP1)-AY(J))/H2
    50 CONTINUE
    S12=S1*S2
C IF DATA IS NOT MONOTONIC SET SLOPE TO ZERO
    IF (S12.GT.0.0)GO TO 10
    G=0.0
    RETURN
    10 CONTINUE
C WHEN DATA IS MONOTONIC USE WEIGHTED AVERAGE OF NORMAL SLOPES
    T1=2.0*H1+H2
    T2=H1+2.0*H2
    T=(T1*S2+T2*S1)/(3.0*(H1+H2))
    G=S12/T
    RETURN
  END

```

CCCCC SUBROUTINE FOR CALCULATING THE ELLIPTIC INTEGRALS USED FOR DETERMINING THE S VALUE FROM THE CURRENT GUESS FOR A/B

```

      REAL FUNCTION FUN(Y)
      COMMON/PARAM/GAMMA(101),T(101),A,C,D,NN,AA(6),AD(6)
      B=1.0
      GOTO(10,20,30,40,50,60,70,80,90),NN
10    FUN=1.0/((A*A+Y)**1.5*(B*B+Y)**0.5*(C*C+Y)**0.5)
      RETURN
20    FUN=1.0/((A*A+Y)**0.5*(B*B+Y)**1.5*(C*C+Y)**0.5)
      RETURN
30    FUN=1.0/((A*A+Y)**0.5*(B*B+Y)**0.5*(C*C+Y)**1.5)
      RETURN
40    FUN=1.0/((A*A+Y)**0.5*(B*B+Y)**1.5*(C*C+Y)**1.5)
      RETURN
50    FUN=1.0/((A*A+Y)**1.5*(B*B+Y)**0.5*(C*C+Y)**1.5)
      RETURN
60    FUN=1.0/((A*A+Y)**1.5*(B*B+Y)**1.5*(C*C+Y)**0.5)
      RETURN
70    FUN=Y/((A*A+Y)**0.5*(B*B+Y)**1.5*(C*C+Y)**1.5)
      RETURN
80    FUN=Y/((A*A+Y)**1.5*(B*B+Y)**0.5*(C*C+Y)**1.5)
      RETURN
90    FUN=Y/((A*A+Y)**1.5*(B*B+Y)**1.5*(C*C+Y)**0.5)
      RETURN
      END

```

Results:

PROTEIN 1, 0.1 DEG. ABSOLUTE ERROR

110NS, 100PTS
STREAM3

FUNCTION VALUE ON EXIT IS .000399962998
A/B= 1.48309 A+= .070458728408 A-= .048831535604

FUNCTION VALUE ON EXIT IS .000399962998
A/B= 1.48309 A+= .070458845275 A-= .048831534073

FUNCTION VALUE ON EXIT IS .000399962998
A/B= 1.48309 A+= .070458881237 A-= .048831534081

BEST LEAST SQUARES VALUE = .000399962998
A / B = 1.48309
A+ = .0707
A- = .0488